

$\Delta(1600) P_{33}$ 

$$I(J^P) = \frac{3}{2}(\frac{3}{2}^+) \text{ Status: } ***$$

Most of the results published before 1975 are now obsolete and have been omitted. They may be found in our 1982 edition, Physics Letters **111B** (1982).

The various analyses are not in good agreement.

### $\Delta(1600)$ BREIT-WIGNER MASS

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1550 to 1700 (<math>\approx</math> 1600) OUR ESTIMATE</b>			
1706 $\pm$ 10	MANLEY	92	IPWA $\pi N \rightarrow \pi N$ & $N\pi\pi$
1600 $\pm$ 50	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
1522 $\pm$ 13	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
1672 $\pm$ 15	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
1706	LI	93	IPWA $\gamma N \rightarrow \pi N$
1690	BARNHAM	80	IPWA $\pi N \rightarrow N\pi\pi$
1560	<sup>1</sup> LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$
1640	<sup>2</sup> LONGACRE	75	IPWA $\pi N \rightarrow N\pi\pi$

### $\Delta(1600)$ BREIT-WIGNER WIDTH

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>250 to 450 (<math>\approx</math> 350) OUR ESTIMATE</b>			
430 $\pm$ 73	MANLEY	92	IPWA $\pi N \rightarrow \pi N$ & $N\pi\pi$
300 $\pm$ 100	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
220 $\pm$ 40	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
315 $\pm$ 20	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
215	LI	93	IPWA $\gamma N \rightarrow \pi N$
250	BARNHAM	80	IPWA $\pi N \rightarrow N\pi\pi$
180	<sup>1</sup> LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$
300	<sup>2</sup> LONGACRE	75	IPWA $\pi N \rightarrow N\pi\pi$

### $\Delta(1600)$ POLE POSITION

#### REAL PART

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1500 to 1700 (<math>\approx</math> 1600) OUR ESTIMATE</b>			
1675	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
1550	<sup>3</sup> HOEHLER	93	SPED $\pi N \rightarrow \pi N$
1550 $\pm$ 40	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
1612	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90
1609 or 1610	<sup>4</sup> LONGACRE	78	IPWA $\pi N \rightarrow N\pi\pi$
1541 or 1542	<sup>1</sup> LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$

**– 2×IMAGINARY PART**

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
<b>200 to 400 (<math>\approx 300</math>) OUR ESTIMATE</b>			
386	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
200±60	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
230	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90
323 or 325	<sup>4</sup> LONGACRE	78	IPWA $\pi N \rightarrow N\pi\pi$
178 or 178	<sup>1</sup> LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$

 **$\Delta(1600)$  ELASTIC POLE RESIDUE**
**MODULUS  $|r|$** 

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
52	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
17±4	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
16	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90
<b>PHASE <math>\theta</math></b>			
VALUE ( $^\circ$ )	DOCUMENT ID	TECN	COMMENT
+ 14	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
– 150±30	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
– 73	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90

 **$\Delta(1600)$  DECAY MODES**

The following branching fractions are our estimates, not fits or averages.

Mode	Fraction ( $\Gamma_i/\Gamma$ )
$\Gamma_1$ $N\pi$	10–25 %
$\Gamma_2$ $\Sigma K$	
$\Gamma_3$ $N\pi\pi$	75–90 %
$\Gamma_4$ $\Delta\pi$	40–70 %
$\Gamma_5$ $\Delta(1232)\pi$ , <i>P</i> -wave	
$\Gamma_6$ $\Delta(1232)\pi$ , <i>F</i> -wave	
$\Gamma_7$ $N\rho$	<25 %
$\Gamma_8$ $N\rho$ , $S=1/2$ , <i>P</i> -wave	
$\Gamma_9$ $N\rho$ , $S=3/2$ , <i>P</i> -wave	
$\Gamma_{10}$ $N\rho$ , $S=3/2$ , <i>F</i> -wave	
$\Gamma_{11}$ $N(1440)\pi$	10–35 %
$\Gamma_{12}$ $N(1440)\pi$ , <i>P</i> -wave	
$\Gamma_{13}$ $N\gamma$	0.001–0.02 %
$\Gamma_{14}$ $N\gamma$ , helicity=1/2	0.0–0.02 %
$\Gamma_{15}$ $N\gamma$ , helicity=3/2	0.001–0.005 %

## Δ(1600) BRANCHING RATIOS

$\Gamma(N\pi)/\Gamma_{\text{total}}$   $\Gamma_1/\Gamma$   
VALUE DOCUMENT ID TECN COMMENT

**0.10 to 0.25 OUR ESTIMATE**

0.12±0.02	MANLEY	92	IPWA	$\pi N \rightarrow \pi N \text{ \& } N\pi\pi$
0.18±0.04	CUTKOSKY	80	IPWA	$\pi N \rightarrow \pi N$
0.21±0.06	HOEHLER	79	IPWA	$\pi N \rightarrow \pi N$

$(\Gamma_i\Gamma_f)^{1/2}/\Gamma_{\text{total}}$  in  $N\pi \rightarrow \Delta(1600) \rightarrow \Sigma K$   $(\Gamma_1\Gamma_2)^{1/2}/\Gamma$   
VALUE DOCUMENT ID TECN COMMENT

**−0.36 to −0.28 OUR ESTIMATE**

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.006 to 0.042	<sup>5</sup> DEANS	75	DPWA	$\pi N \rightarrow \Sigma K$
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Note: Signs of couplings from  $\pi N \rightarrow N\pi\pi$  analyses were changed in the 1986 edition to agree with the baryon-first convention; the overall phase ambiguity is resolved by choosing a negative sign for the  $\Delta(1620) S_{31}$  coupling to  $\Delta(1232)\pi$ .

$(\Gamma_i\Gamma_f)^{1/2}/\Gamma_{\text{total}}$  in  $N\pi \rightarrow \Delta(1600) \rightarrow \Delta(1232)\pi$ , *P-wave*  $(\Gamma_1\Gamma_5)^{1/2}/\Gamma$   
VALUE DOCUMENT ID TECN COMMENT

**+0.27 to +0.33 OUR ESTIMATE**

+0.29±0.02	MANLEY	92	IPWA	$\pi N \rightarrow \pi N \text{ \& } N\pi\pi$
+0.24±0.05	BARNHAM	80	IPWA	$\pi N \rightarrow N\pi\pi$
+0.34	<sup>1,6</sup> LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
+0.30	<sup>2</sup> LONGACRE	75	IPWA	$\pi N \rightarrow N\pi\pi$

$(\Gamma_i\Gamma_f)^{1/2}/\Gamma_{\text{total}}$  in  $N\pi \rightarrow \Delta(1600) \rightarrow \Delta(1232)\pi$ , *F-wave*  $(\Gamma_1\Gamma_6)^{1/2}/\Gamma$   
VALUE DOCUMENT ID TECN COMMENT

**−0.15 to −0.03 OUR ESTIMATE**

−0.07	<sup>1,6</sup> LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
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$(\Gamma_i\Gamma_f)^{1/2}/\Gamma_{\text{total}}$  in  $N\pi \rightarrow \Delta(1600) \rightarrow N\rho$ , *S=1/2, P-wave*  $(\Gamma_1\Gamma_8)^{1/2}/\Gamma$   
VALUE DOCUMENT ID TECN COMMENT

+0.10	<sup>1,6</sup> LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
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$(\Gamma_i\Gamma_f)^{1/2}/\Gamma_{\text{total}}$  in  $N\pi \rightarrow \Delta(1600) \rightarrow N\rho$ , *S=3/2, P-wave*  $(\Gamma_1\Gamma_9)^{1/2}/\Gamma$   
VALUE DOCUMENT ID TECN COMMENT

+0.10	<sup>1,6</sup> LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
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$(\Gamma_i\Gamma_f)^{1/2}/\Gamma_{\text{total}}$  in  $N\pi \rightarrow \Delta(1600) \rightarrow N(1440)\pi$ , *P-wave*  $(\Gamma_1\Gamma_{12})^{1/2}/\Gamma$   
VALUE DOCUMENT ID TECN COMMENT

**+0.15 to +0.23 OUR ESTIMATE**

+0.16±0.02	MANLEY	92	IPWA	$\pi N \rightarrow \pi N \text{ \& } N\pi\pi$
+0.23±0.04	BARNHAM	80	IPWA	$\pi N \rightarrow N\pi\pi$

**$\Delta(1600)$  PHOTON DECAY AMPLITUDES** **$\Delta(1600) \rightarrow N\gamma$ , helicity-1/2 amplitude  $A_{1/2}$** 

<u>VALUE (GeV<sup>-1/2</sup>)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>-0.023±0.020 OUR ESTIMATE</b>			
-0.018±0.015	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
-0.039±0.030	CRAWFORD	83	IPWA $\gamma N \rightarrow \pi N$
-0.046±0.013	AWAJI	81	DPWA $\gamma N \rightarrow \pi N$
0.005±0.020	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
-0.026±0.002	LI	93	IPWA $\gamma N \rightarrow \pi N$
-0.200	<sup>7</sup> WADA	84	DPWA Compton scattering
0.000±0.030	BARBOUR	78	DPWA $\gamma N \rightarrow \pi N$
0.0 ±0.020	FELLER	76	DPWA $\gamma N \rightarrow \pi N$

 **$\Delta(1600) \rightarrow N\gamma$ , helicity-3/2 amplitude  $A_{3/2}$** 

<u>VALUE (GeV<sup>-1/2</sup>)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>-0.009±0.021 OUR ESTIMATE</b>			
-0.025±0.015	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
-0.013±0.014	CRAWFORD	83	IPWA $\gamma N \rightarrow \pi N$
0.025±0.031	AWAJI	81	DPWA $\gamma N \rightarrow \pi N$
-0.009±0.020	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
-0.016±0.002	LI	93	IPWA $\gamma N \rightarrow \pi N$
0.023	WADA	84	DPWA Compton scattering
0.000±0.045	BARBOUR	78	DPWA $\gamma N \rightarrow \pi N$
0.0 ±0.015	FELLER	76	DPWA $\gamma N \rightarrow \pi N$

 **$\Delta(1600)$  FOOTNOTES**

<sup>1</sup> LONGACRE 77 pole positions are from a search for poles in the unitarized T-matrix; the first (second) value uses, in addition to  $\pi N \rightarrow N\pi\pi$  data, elastic amplitudes from a Saclay (CERN) partial-wave analysis. The other LONGACRE 77 values are from eyeball fits with Breit-Wigner circles to the T-matrix amplitudes.

<sup>2</sup> From method II of LONGACRE 75: eyeball fits with Breit-Wigner circles to the T-matrix amplitudes.

<sup>3</sup> See HOEHLER 93 for a detailed discussion of the evidence for and the pole parameters of  $N$  and  $\Delta$  resonances as determined from Argand diagrams of  $\pi N$  elastic partial-wave amplitudes and from plots of the speeds with which the amplitudes traverse the diagrams.

<sup>4</sup> LONGACRE 78 values are from a search for poles in the unitarized T-matrix. The first (second) value uses, in addition to  $\pi N \rightarrow N\pi\pi$  data, elastic amplitudes from a Saclay (CERN) partial-wave analysis.

<sup>5</sup> The range given is from the four best solutions. DEANS 75 disagrees with  $\pi^+ p \rightarrow \Sigma^+ K^+$  data of WINNIK 77 around 1920 MeV.

<sup>6</sup> LONGACRE 77 considers this coupling to be well determined.

<sup>7</sup> WADA 84 is inconsistent with other analyses — see the Note on  $N$  and  $\Delta$  Resonances.

## Δ(1600) REFERENCES

For early references, see Physics Letters **111B** 70 (1982).

ARNDT	96	PR C53 430	+Strakovsky, Workman	(VPI)
ARNDT	95	PR C52 2120	+Strakovsky, Workman, Pavan	(VPI, BRCO)
HOEHLER	93	$\pi$ <i>N</i> Newsletter 9 1		(KARL)
LI	93	PR C47 2759	+Arndt, Roper, Workman	(VPI)
MANLEY	92	PR D45 4002	+Saleski	(KENT) IJP
Also	84	PR D30 904	Manley, Arndt, Goradia, Teplitz	(VPI)
ARNDT	91	PR D43 2131	+Li, Roper, Workman, Ford	(VPI, TELE) IJP
WADA	84	NP B247 313	+Egawa, Imanishi, Ishii, Kato, Ukai+	(INUS)
CRAWFORD	83	NP B211 1	+Morton	(GLAS)
PDG	82	PL 111B	Roos, Porter, Aguilar-Benitez+	(HELS, CIT, CERN)
AWAJI	81	Bonn Conf. 352	+Kajikawa	(NAGO)
Also	82	NP B197 365	Fujii, Hayashii, Iwata, Kajikawa+	(NAGO)
BARNHAM	80	NP B168 243	+Glickman, Mier-Jedrzejowicz+	(LOIC)
CRAWFORD	80	Toronto Conf. 107		(GLAS)
CUTKOSKY	80	Toronto Conf. 19	+Forsyth, Babcock, Kelly, Hendrick	(CMU, LBL) IJP
Also	79	PR D20 2839	Cutkosky, Forsyth, Hendrick, Kelly	(CMU, LBL) IJP
HOEHLER	79	PDAT 12-1	+Kaiser, Koch, Pietarinen	(KARLT) IJP
Also	80	Toronto Conf. 3	Koch	(KARLT) IJP
BARBOUR	78	NP B141 253	+Crawford, Parsons	(GLAS)
LONGACRE	78	PR D17 1795	+Lasinski, Rosenfeld, Smadja+	(LBL, SLAC)
LONGACRE	77	NP B122 493	+Dolbeau	(SACL) IJP
Also	76	NP B108 365	Dolbeau, Triantis, Neveu, Cadiet	(SACL) IJP
WINNIK	77	NP B128 66	+Toaff, Revel, Goldberg, Berny	(HAIF) I
FELLER	76	NP B104 219	+Fukushima, Horikawa, Kajikawa+	(NAGO, OSAK) IJP
DEANS	75	NP B96 90	+Mitchell, Montgomery+	(SFLA, ALAH) IJP
LONGACRE	75	PL 55B 415	+Rosenfeld, Lasinski, Smadja+	(LBL, SLAC) IJP