

$$I(J^P) = \frac{1}{2}(0^-)$$

## $K_S^0$ MEAN LIFE

For earlier measurements, beginning with BOLDT 58B, see our our 1986 edition, Physics Letters **170B** 130 (1986).

OUR FIT is described in the note on "Fits for  $K_L^0$  CP-Violation Parameters" in the  $K_L^0$  Particle Listings.

VALUE ( $10^{-10}$ s)	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.8935 ± 0.0008</b>				<b>OUR FIT</b>
<b>0.8940 ± 0.0009</b>				<b>OUR AVERAGE</b>
0.8971 ± 0.0021		BERTANZA 97	NA31	
0.8941 ± 0.0014 ± 0.0009		SCHWINGEN...95	E773	$\Delta m$ free, $\phi_{+-} = \phi_{SW}$
0.8929 ± 0.0016		GIBBONS 93	E731	
0.8920 ± 0.0044	214k	GROSSMAN 87	SPEC	
0.881 ± 0.009	26k	ARONSON 76	SPEC	
0.8924 ± 0.0032		<sup>1</sup> CARITHERS 75	SPEC	
0.8937 ± 0.0048	6M	GEWENIGER 74B	ASPK	
0.8958 ± 0.0045	50k	<sup>2</sup> SKJEGGEST... 72	HBC	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
0.905 ± 0.007		<sup>3</sup> ARONSON 82B	SPEC	
0.867 ± 0.024	2173	<sup>4</sup> FACKLER 73	OSPK	
0.856 ± 0.008	19994	<sup>5</sup> DONALD 68B	HBC	
0.872 ± 0.009	20000	<sup>5,6</sup> HILL 68	DBC	
0.866 ± 0.016		<sup>5</sup> ALFF-... 66B	OSPK	
0.843 ± 0.013	5000	<sup>5</sup> KIRSCH 66	HBC	

<sup>1</sup>CARITHERS 75 value is for  $m_{K_L^0} - m_{K_S^0}$   $\Delta m = 0.5301 \pm 0.0013$ . The  $\Delta m$  dependence of the total decay rate (inverse mean life) is  $\Gamma(K_S^0) = [(1.122 \pm 0.004) + 0.16(\Delta m - 0.5348)/\Delta m]10^{10}/s$ , or, in terms of meanlife  $\tau_S = 0.8913 \pm 0.0032 - 0.238(\Delta m - 0.5348)$  where  $\Delta m$  and  $\tau_S$  are in units of  $10^{10}\hbar s^{-1}$  and  $10^{-10}s$  respectively.

<sup>2</sup>HILL 68 has been changed by the authors from the published value ( $0.865 \pm 0.009$ ) because of a correction in the shift due to  $\eta_{+-}$ . SKJEGGESTAD 72 and HILL 68 give detailed discussions of systematics encountered in this type of experiment.

<sup>3</sup>ARONSON 82 find that  $K_S^0$  mean life may depend on the kaon energy.

<sup>4</sup>FACKLER 73 does not include systematic errors.

<sup>5</sup>Pre-1971 experiments are excluded from the average because of disagreement with later more precise experiments.

<sup>6</sup>HILL 68 has been changed by the authors from the published value ( $0.865 \pm 0.009$ ) because of a correction in the shift due to  $\eta_{+-}$ . SKJEGGESTAD 72 and HILL 68 give detailed discussions of systematics encountered in this type of experiment.

## $K_S^0$ DECAY MODES

Mode	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level
$\Gamma_1$ $\pi^+ \pi^-$	(68.61 ± 0.28) %	S=1.2
$\Gamma_2$ $\pi^0 \pi^0$	(31.39 ± 0.28) %	S=1.2
$\Gamma_3$ $\pi^+ \pi^- \gamma$	[a,b] ( 1.78 ± 0.05 ) × 10 <sup>-3</sup>	
$\Gamma_4$ $\gamma \gamma$	( 2.4 ± 0.9 ) × 10 <sup>-6</sup>	
$\Gamma_5$ $\pi^+ \pi^- \pi^0$	( 3.2 <sup>+1.2</sup> <sub>-1.0</sub> ) × 10 <sup>-7</sup>	
$\Gamma_6$ $3\pi^0$	< 1.4 × 10 <sup>-5</sup>	CL=90%
$\Gamma_7$ $\pi^\pm e^\mp \nu_e$	[c] ( 7.2 ± 1.4 ) × 10 <sup>-4</sup>	
$\Gamma_8$ $\pi^\pm \mu^\mp \nu_\mu$	[c]	

### $\Delta S = 1$ weak neutral current (S1) modes

$\Gamma_9$ $\mu^+ \mu^-$	S1	< 3.2 × 10 <sup>-7</sup>	CL=90%
$\Gamma_{10}$ $e^+ e^-$	S1	< 1.4 × 10 <sup>-7</sup>	CL=90%
$\Gamma_{11}$ $\pi^0 e^+ e^-$	S1	< 1.1 × 10 <sup>-6</sup>	CL=90%

[a] Most of this radiative mode, the low-momentum  $\gamma$  part, is also included in the parent mode listed without  $\gamma$ 's.

[b] See the Particle Listings below for the energy limits used in this measurement.

[c] The value is for the sum of the charge states or particle/antiparticle states indicated.

## CONSTRAINED FIT INFORMATION

An overall fit to 3 branching ratios uses 17 measurements and one constraint to determine 2 parameters. The overall fit has a  $\chi^2 = 16.5$  for 16 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients  $\langle \delta x_i \delta x_j \rangle / (\delta x_i \delta x_j)$ , in percent, from the fit to the branching fractions,  $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$ . The fit constrains the  $x_i$  whose labels appear in this array to sum to one.

$$x_2 \begin{vmatrix} & -100 \\ & x_1 \end{vmatrix}$$

## $K_S^0$ DECAY RATES

$\Gamma(\pi^\pm e^\mp \nu_e)$				$\Gamma_7$
<u>VALUE (10<sup>6</sup> s<sup>-1</sup>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>8.1 ± 1.6</b>	75	<sup>7</sup> AKHMETSHIN 99	CMD2	Tagged $K_S^0$ using $\phi \rightarrow K_L^0 K_S^0$

• • • We do not use the following data for averages, fits, limits, etc. • • •

7.50 ± 0.08	<sup>8</sup> PDG	98		
seen	BURGUN	72	HBC	$K^+ p \rightarrow K^0 p \pi^+$
9.3 ± 2.5	AUBERT	65	HLBC	$\Delta S = \Delta Q$ , CP cons. not assumed

<sup>7</sup> AKHMETSHIN 99 is from a measured branching ratio  $B(K_S^0 \rightarrow \pi e \nu_e) = (7.2 \pm 1.4) \times 10^{-4}$  and  $\tau_{K_S^0} = (0.8934 \pm 0.0008) \times 10^{-10}$  s.

<sup>8</sup> PDG 98 from  $K_L^0$  measurements, assuming that  $\Delta S = \Delta Q$  in  $K^0$  decay so that  $\Gamma(K_S^0 \rightarrow \pi^\pm e^\mp \nu_e) = \Gamma(K_L^0 \rightarrow \pi^\pm e^\mp \nu_e)$ .

$\Gamma(\pi^\pm \mu^\mp \nu_\mu)$

$\Gamma_8$

VALUE ( $10^6 \text{ s}^{-1}$ )                      DOCUMENT ID

• • • We do not use the following data for averages, fits, limits, etc. • • •

5.25 ± 0.07	<sup>9</sup> PDG	98		
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<sup>9</sup> PDG 98 from  $K_L^0$  measurements, assuming that  $\Delta S = \Delta Q$  in  $K^0$  decay so that  $\Gamma(K_S^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu) = \Gamma(K_L^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu)$ .

## $K_S^0$ BRANCHING RATIOS

$\Gamma(\pi^+ \pi^-) / \Gamma_{\text{total}}$

$\Gamma_1 / \Gamma$

VALUE                      EVTS                      DOCUMENT ID                      TECN                      COMMENT

**0.6861 ± 0.0028 OUR FIT** Error includes scale factor of 1.2.

**0.671 ± 0.010 OUR AVERAGE**

0.670 ± 0.010	3447	<sup>10</sup> DOYLE	69	HBC	$\pi^- p \rightarrow \Lambda K^0$
0.70 ± 0.08		COLUMBIA	60B	HBC	
0.68 ± 0.04		CRAWFORD	59B	HBC	

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.740 ± 0.024		<sup>10</sup> ANDERSON	62B	HBC	
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<sup>10</sup> Anderson result not published, events added to Doyle sample.

$\Gamma(\pi^+ \pi^-) / \Gamma(\pi^0 \pi^0)$

$\Gamma_1 / \Gamma_2$

VALUE                      EVTS                      DOCUMENT ID                      TECN                      COMMENT

**2.186 ± 0.028 OUR FIT** Error includes scale factor of 1.2.

**2.197 ± 0.026 OUR AVERAGE**

2.11 ± 0.09	1315	EVERHART	76	WIRE	$\pi^- p \rightarrow \Lambda K^0$
2.169 ± 0.094	16k	COWELL	74	OSPK	$\pi^- p \rightarrow \Lambda K^0$
2.16 ± 0.08	4799	HILL	73	DBC	$K^+ d \rightarrow K^0 p p$
2.22 ± 0.10	3068	<sup>11</sup> ALITTI	72	HBC	$K^+ p \rightarrow \pi^+ p K^0$
2.22 ± 0.08	6380	MORSE	72B	DBC	$K^+ n \rightarrow K^0 p$
2.10 ± 0.11	701	<sup>12</sup> NAGY	72	HLBC	$K^+ n \rightarrow K^0 p$
2.22 ± 0.095	6150	<sup>13</sup> BALTAY	71	HBC	$K p \rightarrow K^0 \text{ neutrals}$
2.282 ± 0.043	7944	<sup>14</sup> MOFFETT	70	OSPK	$K^+ n \rightarrow K^0 p$
2.10 ± 0.06	3700	MORFIN	69	HLBC	$K^+ n \rightarrow K^0 p$

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.12 ± 0.17	267	<sup>12</sup> BOZOKI	69	HLBC	
2.285 ± 0.055	3016	<sup>14</sup> GOBBI	69	OSPK	$K^+ n \rightarrow K^0 p$

<sup>11</sup> The directly measured quantity is  $K_S^0 \rightarrow \pi^+ \pi^- / \text{all } K^0 = 0.345 \pm 0.005$ .

<sup>12</sup> NAGY 72 is a final result which includes BOZOKI 69.

<sup>13</sup> The directly measured quantity is  $K_S^0 \rightarrow \pi^+ \pi^- / \text{all } \bar{K}^0 = 0.345 \pm 0.005$ .

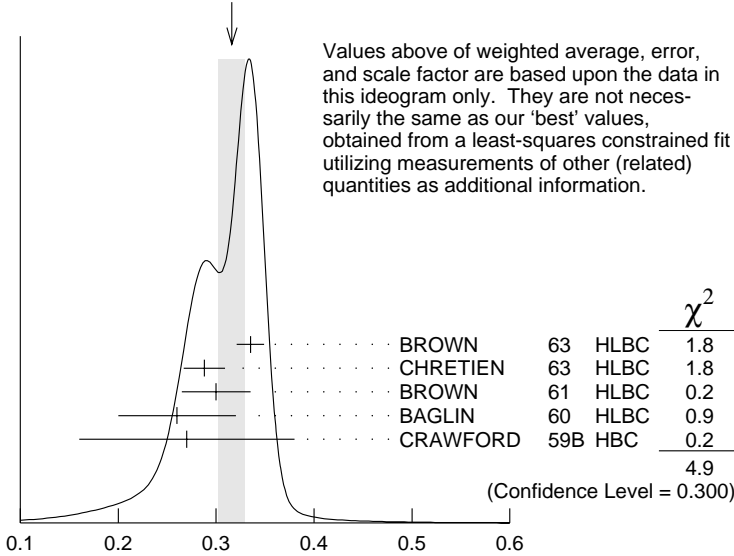
<sup>14</sup> MOFFETT 70 is a final result which includes GOBBI 69.

$\Gamma(\pi^0 \pi^0) / \Gamma_{\text{total}}$

$\Gamma_2 / \Gamma$

VALUE	EVTS	DOCUMENT ID	TECN
<b>0.3139 ± 0.0028 OUR FIT</b>		Error includes scale factor of 1.2.	
<b>0.316 ± 0.014 OUR AVERAGE</b>		Error includes scale factor of 1.3. See the ideogram below.	
0.335 ± 0.014	1066	BROWN	63 HLBC
0.288 ± 0.021	198	CHRETIEN	63 HLBC
0.30 ± 0.035		BROWN	61 HLBC
0.26 ± 0.06		BAGLIN	60 HLBC
0.27 ± 0.11		CRAWFORD	59B HBC

WEIGHTED AVERAGE  
0.316 ± 0.014 (Error scaled by 1.3)



$\Gamma(\pi^0 \pi^0) / \Gamma_{\text{total}}$

$\Gamma(\pi^+ \pi^- \gamma) / \Gamma(\pi^+ \pi^-)$

$\Gamma_3 / \Gamma_1$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.60 ± 0.08 OUR AVERAGE</b>				
2.56 ± 0.09	1286	RAMBERG	93 E731	$p_\gamma > 50$ MeV/c
2.68 ± 0.15		<sup>15</sup> TAUREG	76 SPEC	$p_\gamma > 50$ MeV/c
2.8 ± 0.6		<sup>16</sup> BURGUN	73 HBC	$p_\gamma > 50$ MeV/c
3.3 ± 1.2	10	WEBBER	70 HBC	$p_\gamma > 50$ MeV/c
no ratio given	27	BELLOTTI	66 HBC	$p_\gamma > 50$ MeV/c

• • • We do not use the following data for averages, fits, limits, etc. • • •

7.10±0.22	3723	RAMBERG	93	E731	$p_\gamma > 20 \text{ MeV}/c$
3.0 ±0.6	29	<sup>17</sup> BOBISUT	74	HLBC	$p_\gamma > 40 \text{ MeV}/c$

<sup>15</sup> TAUREG 76 find direct emission contribution <0.06, CL = 90%.

<sup>16</sup> BURGUN 73 estimates that direct emission contribution is  $0.3 \pm 0.6$ .

<sup>17</sup> BOBISUT 74 not included in average because  $p_\gamma$  cut differs. Estimates direct emission contribution to be 0.5 or less, CL = 95%.

$\Gamma(\gamma\gamma)/\Gamma_{\text{total}}$   $\Gamma_4/\Gamma$

VALUE (units $10^{-6}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.4±0.9</b>		35	<sup>18</sup> BARR	95B NA31	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
2.2±1.1		16	<sup>19</sup> BARR	95B NA31	
< 13	90		BALATS	89 SPEC	
2.4±1.2		19	BURKHARDT	87 NA31	
< 133	90		BARMIN	86B XEBC	
< 200	90		VASSERMAN	86 CALO	$\phi \rightarrow K_S^0 K_L^0$
< 400	90	0	BARMIN	73B HLBC	
< 710	90	0	<sup>20</sup> BANNER	72B OSPK	
< 2000	90	0	MORSE	72B DBC	
< 2200	90	0	<sup>20</sup> REPELLIN	71 OSPK	
< 21000	90	0	<sup>20</sup> BANNER	69 OSPK	

<sup>18</sup> BARR 95B quotes this as the combined BARR 95B + BURKHARDT 87 result after rescaling BURKHARDT 87 to use same branching ratios and lifetimes as BARR 95B.

<sup>19</sup> BARR 95B result is calculated using  $B(K_L \rightarrow \gamma\gamma) = (5.86 \pm 0.17) \times 10^{-4}$ .

<sup>20</sup> These limits are for maximum interference in  $K_S^0 - K_L^0$  to  $2\gamma$ 's.

$\Gamma(\pi^+\pi^-\pi^0)/\Gamma_{\text{total}}$   $\Gamma_5/\Gamma$

VALUE (units $10^{-7}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>3.2<sup>+1.2</sup><sub>-1.0</sub> OUR AVERAGE</b>					
2.5 <sup>+1.3+0.5</sup> <sub>-1.0-0.6</sub>		500k	<sup>21</sup> ADLER	97B CPLR	
4.8 <sup>+2.2</sup> <sub>-1.6</sub> ±1.1			<sup>22</sup> ZOU	96 E621	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
4.1 <sup>+2.5+0.5</sup> <sub>-1.9-0.6</sub>			<sup>23</sup> ADLER	96E CPLR	Sup. by ADLER 97B
3.9 <sup>+5.4+0.9</sup> <sub>-1.8-0.7</sub>			<sup>24</sup> THOMSON	94 E621	Sup. by ZOU 96
<490	90		<sup>25</sup> BARMIN	85 HLBC	
<850	90		METCALF	72 ASPK	

<sup>21</sup> ADLER 97B find the  $CP$ -conserving parameters  $\text{Re}(\lambda) = (28 \pm 7 \pm 3) \times 10^{-3}$ ,  $\text{Im}(\lambda) = (-10 \pm 8 \pm 2) \times 10^{-3}$ . They estimate  $B(K_S^0 \rightarrow \pi^+\pi^-\pi^0)$  from  $\text{Re}(\lambda)$  and the  $K_L^0$  decay parameters. See also ANGELOPOULOS 98C.

<sup>22</sup> ZOU 96 is from the the measured quantities  $|\rho_{+-0}| = 0.039^{+0.009}_{-0.006} \pm 0.005$  and  $\phi_\rho = (-9 \pm 18)^\circ$ .

<sup>23</sup> ADLER 96E is from the measured quantities  $\text{Re}(\lambda) = 0.036 \pm 0.010^{+0.002}_{-0.003}$  and  $\text{Im}(\lambda)$  consistent with zero. Note that the quantity  $\lambda$  is the same as  $\rho_{+-0}$  used in other footnotes.

<sup>24</sup> THOMSON 94 calculates this branching ratio from their measurements  $|\rho_{+-0}| = 0.035^{+0.019}_{-0.011} \pm 0.004$  and  $\phi_\rho = (-59 \pm 48)^\circ$  where  $|\rho_{+-0}| e^{i\phi_\rho} = A(K_S^0 \rightarrow \pi^+ \pi^- \pi^0, I=2)/A(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)$ .

<sup>25</sup> BARMIN 85 assumes that *CP*-allowed and *CP*-violating amplitudes are equally suppressed.

**$\Gamma(3\pi^0)/\Gamma_{\text{total}}$**   **$\Gamma_6/\Gamma$**

Violates *CP* conservation.

VALUE (units $10^{-5}$ )	CL%	EVTS	DOCUMENT ID	TECN
<b>&lt; 1.4</b>	90	7M	ACHASOV	99D SND
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
< 1.9	90	17300	<sup>26</sup> ANGELOPO...	98B CPLR
< 3.7	90		BARMIN	83 HLBC
< 43	90		BARMIN	73 HLBC

<sup>26</sup> ANGELOPOULOS 98B is from  $\text{Im}(\eta_{000}) = -0.05 \pm 0.12 \pm 0.05$ , assuming  $\text{Re}(\eta_{000}) = \text{Re}(\epsilon) = 1.635 \times 10^{-3}$  and using the value  $B(K_L^0 \rightarrow \pi^0 \pi^0 \pi^0) = 0.2112 \pm 0.0027$ .

**$\Gamma(\pi^\pm e^\mp \nu_e)/\Gamma_{\text{total}}$**   **$\Gamma_7/\Gamma$**

VALUE (units $10^{-4}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>7.2 ± 1.4</b>	75	AKHMETSHIN 99	CMD2	Tagged $K_S^0$ using $\phi \rightarrow K_L^0 K_S^0$

**$\Gamma(\mu^+ \mu^-)/\Gamma_{\text{total}}$**   **$\Gamma_9/\Gamma$**

Test for  $\Delta S = 1$  weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

VALUE (units $10^{-5}$ )	CL%	DOCUMENT ID	TECN
<b>&lt; 0.032</b>	90	GJESDAL	73 ASPK
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
< 14	90	BOHM	69 OSPK
< 0.7	90	HYAMS	69B OSPK
< 22	90	<sup>27</sup> STUTZKE	69 OSPK
< 7	90	BOTT-...	67 OSPK

<sup>27</sup> Value calculated by us, using 2.3 instead of 1 event, 90% CL.

**$\Gamma(e^+ e^-)/\Gamma_{\text{total}}$**   **$\Gamma_{10}/\Gamma$**

Test for  $\Delta S = 1$  weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

VALUE (units $10^{-7}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>&lt; 1.4</b>	90		ANGELOPO...	97	CPLR
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
< 28	90	0	BLICK	94	CNTR Hyperon facility
< 100	90		BARMIN	86	XEBC
< 1100	90		BITSADZE	86	CALO
< 3400	90		BOHM	69	OSPK

$\Gamma(\pi^0 e^+ e^-)/\Gamma_{\text{total}}$	$\Gamma_{11}/\Gamma$			
Test for $\Delta S = 1$ weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.				
<u>VALUE (units <math>10^{-6}</math>)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
< <b>1.1</b>	90	0	BARR	93B NA31
• • • We do not use the following data for averages, fits, limits, etc. • • •				
<45	90		GIBBONS	88 E731

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## CP VIOLATION IN $K_S \rightarrow 3\pi$

Written 1996 by T. Nakada (Paul Scherrer Institute) and L. Wolfenstein (Carnegie-Mellon University).

The possible final states for the decay  $K^0 \rightarrow \pi^+ \pi^- \pi^0$  have isospin  $I = 0, 1, 2$ , and  $3$ . The  $I = 0$  and  $I = 2$  states have  $CP = +1$  and  $K_S$  can decay into them without violating  $CP$  symmetry, but they are expected to be strongly suppressed by centrifugal barrier effects. The  $I = 1$  and  $I = 3$  states, which have no centrifugal barrier, have  $CP = -1$  so that the  $K_S$  decay to these requires  $CP$  violation.

In order to see  $CP$  violation in  $K_S \rightarrow \pi^+ \pi^- \pi^0$ , it is necessary to observe the interference between  $K_S$  and  $K_L$  decay, which determines the amplitude ratio

$$\eta_{+-0} = \frac{A(K_S \rightarrow \pi^+ \pi^- \pi^0)}{A(K_L \rightarrow \pi^+ \pi^- \pi^0)}. \quad (1)$$

If  $\eta_{+-0}$  is obtained from an integration over the whole Dalitz plot, there is no contribution from the  $I = 0$  and  $I = 2$  final states and a nonzero value of  $\eta_{+-0}$  is entirely due to  $CP$  violation.

Only  $I = 1$  and  $I = 3$  states, which are  $CP = -1$ , are allowed for  $K^0 \rightarrow \pi^0 \pi^0 \pi^0$  decays and the decay of  $K_S$  into  $3\pi^0$  is an unambiguous sign of  $CP$  violation. Similarly to  $\eta_{+-0}$ ,  $\eta_{000}$  is defined as

$$\eta_{000} = \frac{A(K_S \rightarrow \pi^0 \pi^0 \pi^0)}{A(K_L \rightarrow \pi^0 \pi^0 \pi^0)}. \quad (2)$$

If one assumes that  $CPT$  invariance holds and that there are no transitions to  $I = 3$  (or to nonsymmetric  $I = 1$  states), it can be shown that

$$\begin{aligned} \eta_{+-0} &= \eta_{000} \\ &= \epsilon + i \frac{\text{Im } a_1}{\text{Re } a_1} . \end{aligned} \quad (3)$$

With the Wu-Yang phase convention,  $a_1$  is the weak decay amplitude for  $K^0$  into  $I = 1$  final states;  $\epsilon$  is determined from  $CP$  violation in  $K_L \rightarrow 2\pi$  decays. The real parts of  $\eta_{+-0}$  and  $\eta_{000}$  are equal to  $\text{Re}(\epsilon)$ . Since currently-known upper limits on  $|\eta_{+-0}|$  and  $|\eta_{000}|$  are much larger than  $|\epsilon|$ , they can be interpreted as upper limits on  $\text{Im}(\eta_{+-0})$  and  $\text{Im}(\eta_{000})$  and so as limits on the  $CP$ -violating phase of the decay amplitude  $a_1$ .

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### CP-VIOLATION PARAMETERS IN $K_S^0$ DECAY

$\text{Im}(\eta_{+-0})^2 = \Gamma(K_S^0 \rightarrow \pi^+ \pi^- \pi^0, CP\text{-violating}) / \Gamma(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)$   
*CPT* assumed valid (i.e.  $\text{Re}(\eta_{+-0}) \simeq 0$ ).

VALUE	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
<0.23	90	601	<sup>28</sup> BARMIN	85	HLBC
<1.2	90	192	BALDO-...	75	HLBC
<0.71	90	148	MALLARY	73	OSPK Re(A) = -0.05 ± 0.17
<0.66	90	180	JAMES	72	HBC
<1.2	90	99	JONES	72	OSPK
<0.12	90	384	METCALF	72	ASPK
<1.2	90	99	CHO	71	DBC
<1.0	90	98	JAMES	71	HBC Incl. in JAMES 72
<1.2	95	50	<sup>29</sup> MEISNER	71	HBC CL=90% not avail.
<0.8	90	71	WEBBER	70	HBC
<0.45	90		BEHR	66	HLBC
<3.8	90	18	ANDERSON	65	HBC Incl. in WEBBER 70

<sup>28</sup> BARMIN 85 find  $\text{Re}(\eta_{+-0}) = (0.05 \pm 0.17)$  and  $\text{Im}(\eta_{+-0}) = (0.15 \pm 0.33)$ . Includes events of BALDO-CEOLIN 75.

<sup>29</sup> These authors find  $\text{Re}(A) = 2.75 \pm 0.65$ , above value at  $\text{Re}(A) = 0$ .



**$\text{Im}(\eta_{+-0}) = \text{Im}(A(K_S^0 \rightarrow \pi^+ \pi^- \pi^0), \text{CP-violating}) / A(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)$**

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
$-0.002 \pm 0.009^{+0.002}_{-0.001}$	500k	30 ADLER	97B CPLR	

• • • We do not use the following data for averages, fits, limits, etc. • • •

$-0.002 \pm 0.018 \pm 0.003$	137k	31 ADLER	96D CPLR	Sup. by ADLER 97B
$-0.015 \pm 0.017 \pm 0.025$	272k	32 ZOU	94 SPEC	

<sup>30</sup> ADLER 97B also find  $\text{Re}(\eta_{+-0}) = -0.002 \pm 0.007^{+0.004}_{-0.001}$ . See also ANGELOPOULOS 98C.

<sup>31</sup> The ADLER 96D fit also yields  $\text{Re}(\eta_{+-0}) = 0.006 \pm 0.013 \pm 0.001$  with a correlation +0.66 between real and imaginary parts. Their results correspond to  $|\eta_{+-0}| < 0.037$  with 90% CL.

<sup>32</sup> ZOU 94 use theoretical constraint  $\text{Re}(\eta_{+-0}) = \text{Re}(\epsilon) = 0.0016$ . Without this constraint they find  $\text{Im}(\eta_{+-0}) = 0.019 \pm 0.061$  and  $\text{Re}(\eta_{+-0}) = 0.019 \pm 0.027$ .

**$\text{Im}(\eta_{000})^2 = \Gamma(K_S^0 \rightarrow 3\pi^0) / \Gamma(K_L^0 \rightarrow 3\pi^0)$**

*CPT* assumed valid (i.e.  $\text{Re}(\eta_{000}) \simeq 0$ ). This limit determines branching ratio  $\Gamma(3\pi^0)/\Gamma_{\text{total}}$  above.

<u>VALUE</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<0.1	90	632	33 BARMIN	83 HLBC	
<0.28	90		34 GJESDAL	74B SPEC	Indirect meas.
<1.2	90	22	BARMIN	73 HLBC	

<sup>33</sup> BARMIN 83 find  $\text{Re}(\eta_{000}) = (-0.08 \pm 0.18)$  and  $\text{Im}(\eta_{000}) = (-0.05 \pm 0.27)$ . Assuming *CPT* invariance they obtain the limit quoted above.

<sup>34</sup> GJESDAL 74B uses  $K2\pi$ ,  $K_{\mu 3}$ , and  $K_{e3}$  decay results, unitarity, and *CPT*. Calculates  $|\eta_{000}| = 0.26 \pm 0.20$ . We convert to upper limit.

**$\text{Im}(\eta_{000}) = \text{Im}(A(K_S^0 \rightarrow \pi^0 \pi^0 \pi^0) / A(K_L^0 \rightarrow \pi^0 \pi^0 \pi^0))$**

$K_S^0 \rightarrow \pi^0 \pi^0 \pi^0$  violates *CP* conservation, in contrast to  $K_S^0 \rightarrow \pi^+ \pi^- \pi^0$  which has a *CP*-conserving part.

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
$-0.05 \pm 0.12 \pm 0.05$	17300	35 ANGELOPO...	98B CPLR

<sup>35</sup> ANGELOPOULOS 98B assumes  $\text{Re}(\eta_{000}) = \text{Re}(\epsilon) = 1.635 \times 10^{-3}$ . Without assuming *CPT* invariance, they obtain  $\text{Re}(\eta_{000}) = 0.18 \pm 0.14 \pm 0.06$  and  $\text{Im}(\eta_{000}) = 0.15 \pm 0.20 \pm 0.03$ .

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