LIGHT QUARKS (u, d, s)

OMITTED FROM SUMMARY TABLE

u-QUARK MASS

The u-, d-, and s-quark masses are estimates of so-called "current-quark masses," in a mass- independent subtraction scheme such as $\overline{\rm MS}$. The ratios m_u/m_d and m_s/m_d are extracted from pion and kaon masses using chiral symmetry. The estimates of d and u masses are not without controversy and remain under active investigation. Within the literature there are even suggestions that the u quark could be essentially massless. The s-quark mass is estimated from SU(3) splittings in hadron masses.

We have normalized the $\overline{\rm MS}$ masses at a renormalization scale of $\mu=2$ GeV. Results quoted in the literature at $\mu=1$ GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV) DOCUMENT ID TECN COMMENT

1.5 to 4.0 OUR EVALUATION

● We do not use the following data for averages, fits, limits, etc.

1.7 ± 0.3	¹ AUBIN	04A LATT	MS scheme
2.9 ± 0.6	² JAMIN	02 THEO	MS scheme
2.3 ± 0.4	³ NARISON	99 THEO	MS scheme
3.9 ± 1.1	⁴ JAMIN	95 THEO	MS scheme
3.0 ± 0.7	⁵ NARISON	95c THEO	MS scheme

¹ AUBIN 04A employ a partially quenched lattice calculation of the pseudoscalar meson masses.

d-QUARK MASS

See the comment for the u quark above.

We have normalized the $\overline{\rm MS}$ masses at a renormalization scale of $\mu=2$ GeV. Results quoted in the literature at $\mu=1$ GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV) DOCUMENT ID TECN COMMENT

4 to 8 OUR EVALUATION

• • • We do not use the following data for averages, fits, limits, etc. • • •

masses. 2 JAMIN 02 first calculates the strange quark mass from QCD sum rules using the scalar channel, and then combines with the quark mass ratios obtained from chiral perturbation theory to obtain $m_{\rm u}$.

³ NARISON 99 uses sum rules to order α_s^3 for ϕ meson decays to get m_s , and finds m_u by combining with sum rule estimates of $m_u + m_d$ and Dashen's formula.

⁴ JAMIN 95 uses QCD sum rules at next-to-leading order. We have rescaled $m_u(1~{\rm GeV})$ = 5.3 \pm 1.5 to μ = 2 GeV.

 $^{^{5}}$ For NARISON 95C, we have rescaled $m_{_{\mbox{\it U}}}(1\,\mbox{GeV})=4\pm1$ to $\mu=2\,\mbox{GeV}.$

3.9 ± 0.5	⁶ AUBIN	04A LATT	MS scheme
$5.2 \!\pm\! 0.9$	⁷ JAMIN	02 THEO	MS scheme
6.4 ± 1.1	⁸ NARISON	99 THEO	MS scheme
7.0 ± 1.1	⁹ JAMIN	95 THEO	MS scheme
7.4 ± 0.7	¹⁰ NARISON	95C THEO	MS scheme

⁶ AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses, and one-loop perturbative renormalization constant.

$\overline{m} = (m_u + m_d)/2$

See the comments for the u quark above.

We have normalized the $\overline{\rm MS}$ masses at a renormalization scale of $\mu=2$ GeV. Results quoted in the literature at $\mu=1$ GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID		TECN	COMMENT
3.0 to 5.5 OUR EVALUATION				
• • • We do not use the followin		, fits,	, limits,	etc. • • •
2.8 ± 0.3	¹¹ AUBIN	04	LATT	MS scheme
$4.29 \pm 0.14 \pm 0.65$	¹² AOKI	03	LATT	MS scheme
$3.223 ^{+ 0.046}_{- 0.069}$	¹³ AOKI	03 B	LATT	MS scheme
$4.4 \pm 0.1 \pm 0.4$	¹⁴ BECIREVIC	03	LATT	MS scheme
$4.1 \pm 0.3 \pm 1.0$	¹⁵ CHIU	03	LATT	MS scheme
$\begin{array}{cc} 3.45 & +0.14 \\ -0.20 \end{array}$	¹⁶ ALIKHAN	02	LATT	MS scheme
5.3 ± 0.3	¹⁷ CHIU	02	LATT	MS scheme
3.9 ± 0.6	¹⁸ MALTMAN	02	THEO	MS scheme
3.9 ± 0.6	¹⁹ MALTMAN	01	THEO	MS scheme
4.57 ± 0.18	²⁰ AOKI	00	LATT	MS scheme
4.4 ± 2	²¹ GOECKELER	00	LATT	MS scheme
4.23 ± 0.29	²² AOKI	99	LATT	MS scheme
≥ 2.1	²³ STEELE	99	THEO	MS scheme
4.5 ± 0.4	²⁴ BECIREVIC	98	LATT	MS scheme
4.6 ± 1.2	²⁵ DOSCH	98	THEO	MS scheme
4.7 ± 0.9	²⁶ PRADES	98	THEO	MS scheme
2.7 ± 0.2	²⁷ EICKER	97	LATT	MS scheme
3.6 ± 0.6	²⁸ GOUGH	97	LATT	MS scheme
$3.4 \pm 0.4 \pm 0.3$	²⁹ GUPTA	97	LATT	MS scheme
>3.8	30 LELLOUCH	97	THEO	MS scheme
4.5 ± 1.0	³¹ BIJNENS	95	THEO	MS scheme

HTTP://PDG.LBL.GOV

 $^{^7}$ JAMIN 02 first calculates the strange quark mass from QCD sum rules using the scalar channel, and then combines with the quark mass ratios obtained from chiral perturbation theory to obtain m_d .

⁸ NARISON 99 uses sum rules to order α_s^3 for ϕ meson decays to get m_s , and finds m_d by combining with sum rule estimates of $m_u + m_d$ and Dashen's formula.

 $^{^9}$ JAMIN 95 uses QCD sum rules at next-to-leading order. We have rescaled $m_d(1\,{\rm GeV})$ = 9.4 \pm 1.5 to μ = 2 GeV.

 $^{^{10}}$ For NARISON 95C, we have rescaled $m_d(1\,{
m GeV})=10\pm1$ to $\mu=2\,{
m GeV}.$

- ¹¹ AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.
- ¹² AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory.
- ¹³ AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the $\mathcal{O}(a)$ improved Wilson action.
- ¹⁴ BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses $\mathcal{O}(a)$ improved Wilson action and nonperturbative renormalization.
- ¹⁵CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.
- 16 ALIKHAN 02 uses lattice simulation of the meson and baryon masses with two dynamical flavors and degenerate light quarks.
- ¹⁷ CHIU 02 extracts the average light quark mass from quenched lattice simulations using quenched chiral perturbation theory.
- ¹⁸ MALTMAN 02 uses finite energy sum rules in the *ud* and *us* pseudoscalar channels. Other mass values are also obtained by similar methods.
- $^{
 m 19}$ MALTMAN 01 uses Borel transformed and finite energy sum rules.
- ²⁰ AOKI 00 obtain the light quark masses from a quenched lattice simulation of the meson and baryon spectrum with the Wilson quark action.
- ²¹ GOECKELER 00 obtained from a quenched lattice computation of the pseudoscalar meson masses using $\mathcal{O}(a)$ improved Wilson fermions and nonperturbative renormalization.
- ²² AOKI 99 obtain the light quark masses from a quenched lattice simulation of the meson spectrum with the staggered quark action employing the regularization independent scheme.
- ²³ STEELE 99 obtain a bound on the light quark masses by applying the Holder inequality to a sum rule. We have converted their bound of $(m_u+m_d)/2 \ge 3$ MeV at $\mu=1$ GeV to $\mu=2$ GeV.
- 24 BECIREVIC 98 compute the quark mass using the Alpha action in the quenched approximation. The conversion from the regularization independent scheme to the MS scheme is at NNLO.
- ²⁵ DOSCH 98 use sum rule determinations of the quark condensate and chiral perturbation theory to obtain $9.4 \le (m_u + m_d)(1 \text{ GeV}) \le 15.7 \text{ MeV}$. We have converted to result to u=2 GeV.
- ²⁶ PRADES 98 uses finite energy sum rules for the axial current correlator.
- 27 EICKER 97 use lattice gauge computations with two dynamical light flavors.
- ²⁸ GOUGH 97 use lattice gauge computations in the quenched approximation. Correcting for quenching gives $2.1 < \overline{m} < 3.5$ MeV at μ =2 GeV.
- ²⁹ GUPTA 97 use Lattice Monte Carlo computations in the quenched approximation. The value for two light dynamic flavors at $\mu=2$ GeV is 2.7 \pm 0.3 \pm 0.3 MeV.
- ³⁰ LELLOUCH 97 obtain lower bounds on quark masses using hadronic spectral functions.
- ³¹ BIJNENS 95 determines $m_u + m_d$ (1 GeV) = 12 \pm 2.5 MeV using finite energy sum rules. We have rescaled this to 2 GeV.

s-QUARK MASS

See the comment for the u quark above.

We have normalized the $\overline{\rm MS}$ masses at a renormalization scale of $\mu=2$ GeV. Results quoted in the literature at $\mu=1$ GeV have been rescaled by dividing by 1.35.

VALUE (MeV) DOCUMENT ID TECN COMMENT

80 to 130 OUR EVALUATION

• • • We do not use the following data for averages, fits, limits, etc. • • •

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76 ± 8 $116 \pm 6 \pm 0.65$	³² AUBIN ³³ AOKI		LATT LATT	MS scheme
$84.5 + 12 \\ -1.7$	³⁴ AOKI	03 B	LATT	MS scheme
$106 \pm 2 \pm 8$ $92 \pm 9 \pm 16$ 117 ± 17 103 ± 17	35 BECIREVIC 36 CHIU 37 GAMIZ 38 GAMIZ	03	LATT LATT THEO THEO	MS scheme MS scheme MS scheme MS scheme
$88 \begin{array}{c} + \ 3 \\ - \ 6 \end{array}$	³⁹ ALIKHAN	02	LATT	MS scheme
115 ± 8 99 ± 16 100 ± 12	40 CHIU 41 JAMIN 42 MALTMAN 43 CHEN	02 02	LATT THEO THEO	MS scheme MS scheme MS scheme
-25			THEO	MS scheme
125 ± 27 130 ± 15 105 ± 4 118 ± 14	44 KOERNER 45 AOKI 46 GOECKELER 47 AOKI	00 00	THEO LATT LATT LATT	MS scheme MS scheme MS scheme MS scheme
$170 \begin{array}{c} +44 \\ -55 \end{array}$	⁴⁸ BARATE	99R	ALEP	MS scheme
115 ± 8 129 ± 24 114 ± 23 111 ± 12 148 ± 48 103 ± 10 115 ± 19 152.4 ± 14.1 ≥ 89 140 ± 20 95 ± 16	49 MALTMAN 50 NARISON 51 PICH 52 BECIREVIC 53 CHETYRKIN 54 CUCCHIERI 55 DOMINGUEZ 56 CHETYRKIN 57 COLANGELO 58 EICKER 59 GOUGH	99 99 98 98 98 97 97	THEO THEO THEO LATT THEO LATT THEO THEO THEO LATT LATT	MS scheme
$100 \pm 21 \pm 10$ >100 140 ± 24	60 GUPTA 61 LELLOUCH 62 JAMIN		LATT THEO THEO	MS scheme MS scheme MS scheme

³² AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.

 34 AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the $\mathcal{O}(a)$ improved Wilson action.

 $^{^{33}}$ AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory. Determines $\rm m_s\!=\!113.8\pm2.3^{+5.8}_{-2.9}$ using K mass as input and $\rm m_s\!=\!142.3\pm5.8^{+22}_{-0}$ using ϕ mass as input. We have performed a weighted average of these values.

³⁵ BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses $\mathcal{O}(a)$ improved Wilson action and nonperturbative renormalization. They also quote \overline{m}/m_s =24.3 \pm 0.2 \pm 0.6.

³⁶CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.

 $^{^{37}}$ GAMIZ 03 determines m_s from SU(3) breaking in the τ hadronic width. The value of $V_{u\,s}$ is chosen to satisfy CKM unitarity.

 $^{^{38}\,\}mathrm{GAMIZ}$ 03 determines m_{S} from SU(3) breaking in the τ hadronic width. The value of V_{US} is taken from the PDG.

- 39 ALIKHAN 02 uses lattice simulation of the meson and baryon masses with two dynamical flavors and degenerate light quarks. The above value uses the K-meson mass to determine m_s . If the ϕ meson is used, the number changes to $90^+_{-10}^{5}$.
- ⁴⁰ CHIU 02 extracts the strange quark mass from quenched lattice simulations using quenched chiral perturbation theory.
- 41 JAMIN 02 calculates the strange quark mass from QCD sum rules using the scalar channel.
- 42 MALTMAN 02 uses finite energy sum rules in the *ud* and *us* pseudoscalar channels. Other mass values are also obtained by similar methods.
- 43 CHEN 01B uses an analysis of the hadronic spectral function in au decay.
- ⁴⁴ KOERNER 01 obtain the s quark mass of $m_s(m_\tau)=130\pm27(\text{exp})\pm9(\text{thy})$ MeV from an analysis of Cabibbo suppressed τ decays. We have converted this to $\mu=2$ GeV.
- 45 AOKI 00 obtain the light quark masses from a quenched lattice simulation of the meson and baryon spectrum with the Wilson quark action. We have averaged their results of $m_{\rm S} = 115.6 \pm 2.3$ and $m_{\rm S} = 143.7 \pm 5.8$ obtained using $m_{\rm K}$ and m_{ϕ} , respectively, to normalize the spectrum.
- ⁴⁶ GOECKELER 00 obtained from a quenched lattice computation of the pseudoscalar meson masses using $\mathcal{O}(a)$ improved Wilson fermions and nonperturbative renormalization.
- ⁴⁷ AOKI 99 obtain the light quark masses from a quenched lattice simulation of the meson spectrum with the Staggered quark action employing the regularization independent scheme. We have averaged their results of m_{s} =106.0 \pm 7.1 and m_{s} =129 \pm 12 obtained using m_{K} and m_{ϕ} , respectively, to normalize the spectrum.
- ⁴⁸ BARATE 99R obtain the strange quark mass from an analysis of the observed mass spectra in τ decay. We have converted their value of $m_S(m_\tau) = 176 {+46 \atop -57}$ MeV to $\mu = 2$ GeV.
- 49 MALTMAN 99 determines the strange quark mass using finite energy sum rules.
- 50 NARISON 99 uses sum rules to order $lpha_{
 m s}^{3}$ for ϕ meson decays.
- 51 PICH 99 obtain the s-quark mass from an analysis of the moments of the invariant mass distribution in τ decays.
- 52 BECIREVIC 98 compute the quark mass using the Alpha action in the quenched approximation. The conversion from the regularization independent scheme to the MS scheme is at NNLO.
- ⁵³ CHETYRKIN 98 uses spectral moments of hadronic τ decays to determine $m_s(1\,\text{GeV})=200\pm70\,\text{MeV}$. We have rescaled the result to $\mu=2\,\text{GeV}$.
- 54 CUCCHIERI 98 obtains the quark mass using a quenched lattice computation of the hadronic spectrum.
- ⁵⁵ DOMINGUEZ 98 uses hadronic spectral function sum rules (to four loops, and including dimension six operators) to determine $m_{\rm S}(1~{\rm GeV})<155\pm25~{\rm MeV}$. We have rescaled the result to μ =2 GeV.
- 56 CHETYRKIN 97 obtains 205.5 \pm 19.1 MeV at $\mu{=}1$ GeV from QCD sum rules including fourth-order QCD corrections. We have rescaled the result to 2 GeV.
- 57 COLANGELO 97 is QCD sum rule computation. We have rescaled $m_{\rm S}(1~{\rm GeV})>120$ to $\mu=2~{\rm GeV}.$
- ⁵⁸ EICKER 97 use lattice gauge computations with two dynamical light flavors.
- 59 GOUGH 97 use lattice gauge computations in the quenched approximation. Correcting for quenching gives 54 $<\!m_S^{}<\!92$ MeV at $\mu{=}2$ GeV.
- 60 GUPTA 97 use Lattice Monte Carlo computations in the quenched approximation. The value for two light dynamical flavors at $\mu=2$ GeV is $68\pm12\pm7$ MeV.
- ⁶¹ LELLOUCH 97 obtain lower bounds on quark masses using hadronic spectral functions.
- ⁶² JAMIN 95 uses QCD sum rules at next-to-leading order. We have rescaled $m_{\rm S}(1~{\rm GeV})$ = 189 \pm 32 to μ = 2 GeV.

LIGHT QUARK MASS RATIOS

u/d MASS RATIO

<u>VALUE</u>		DOCUMENT ID	<u>TECN</u>	COMMENT
Λ 2	+- A 7 ALID EVALUATION			

0.3 to 0.7 OUR EVALUATION

• • We do not use the following data for averages, fits, limits, etc.

$0.43\ \pm0.08$	⁶³ AUBIN	04A LATT	MS scheme
0.410 ± 0.036		03 LATT	MS scheme
0.44	⁶⁵ GAO		MS scheme
0.553 ± 0.043	66 LEUTWYLER	96 THEO	Compilation
< 0.3	⁶⁷ CHOI	92 THEO	
0.26	⁶⁸ DONOGHUE	92 THEO	
0.30 ± 0.07	⁶⁹ DONOGHUE		
0.66	⁷⁰ GERARD	90 THEO	
0.4 to 0.65	⁷¹ LEUTWYLER		
0.05 to 0.78	⁷² MALTMAN	90 THEO	

⁶³ AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses.

s/d MASS RATIO

17 . 00 OUD EVALUATION			
VALUE	DOCUMENT ID	TECN	COMMENT

17 to 22 OUR EVALUATION

• • • We do not use the following data for averages, fits, limits, etc. • • •

20.0	⁷³ GAO			
18.9 ± 0.8	⁷⁴ LEUTWYLER			Compilation
21	⁷⁵ DONOGHUE	92	THEO	
18	⁷⁶ GERARD	90	THEO	
18 to 23	⁷⁷ LEUTWYLER	90 B	THEO	

 $^{^{64}}$ NELSON 03 computes coefficients in the order p^4 chiral Lagrangian using a lattice calculation with three dynamical flavors. The ratio m_u/m_d is obtained by combining this with the chiral perturbation theory computation of the meson masses to order p^4 .

 $^{^{65}\,\}mathrm{GAO}$ 97 uses electromagnetic mass splittings of light mesons.

⁶⁶ LEUTWYLER 96 uses a combined fit to $\eta \to 3\pi$ and $\psi' \to J/\psi$ (π,η) decay rates, and the electromagnetic mass differences of the π and K.

⁶⁷ CHOI 92 result obtained from the decays $\psi(2S) \to J/\psi(1S)\pi$ and $\psi(2S) \to J/\psi(1S)\eta$, and a dilute instanton gas estimate of some unknown matrix elements.

⁶⁸ DONOGHUE 92 result is from a combined analysis of meson masses, $\eta \to 3\pi$ using second-order chiral perturbation theory including nonanalytic terms, and $(\psi(2S) \to J/\psi(1S)\pi)/(\psi(2S) \to J/\psi(1S)\eta)$.

⁶⁹ DONOGHUE 92B computes quark mass ratios using $(\psi(2S) \to J/\psi(1S)\pi)/(\psi(2S) \to J/\psi(1S)\eta)$, and an estimate of L_{14} using Weinberg sum rules.

⁷⁰ GERARD 90 uses large N and η - η' mixing.

 $^{^{71}}$ LEUTWYLER 90B determines quark mass ratios using second-order chiral perturbation theory for the meson and baryon masses, including nonanalytic corrections. Also uses Weinberg sum rules to determine L_7 .

⁷² MALTMAN 90 uses second-order chiral perturbation theory including nonanalytic terms for the meson masses. Uses a criterion of "maximum reasonableness" that certain coefficients which are expected to be of order one are < 3.

m_s/\overline{m} MASS RATIO

$$\overline{m} \equiv (m_{\mu} + m_{d})/2$$

VALUE DOCUMENT ID TECN

25 to 30 OUR EVALUATION

• • We do not use the following data for averages, fits, limits, etc. • •

 27.4 ± 0.4

⁷⁸ AUBIN

04 LATT

Q MASS RATIO

$$Q \equiv \sqrt{(m_s^2 - \overline{m}^2)/(m_d^2 - m_s^2)}; \quad \overline{m} \equiv (m_u + m_d)/2$$

VALUE DOCUMENT ID TECN

• • • We do not use the following data for averages, fits, limits, etc. • •

 22.8 ± 0.4 22.7 ± 0.8 ⁷⁹ MARTEMYAN.05 THEO ⁸⁰ ANISOVICH 96 THEO

LIGHT QUARKS (u, d, s) REFERENCES

MARTEMYAN0)5	PR D71 017501	B.V. Martemyanov, V.S. Sopov	
AUBIN 0)4	PR D70 031504R	C. Aubin et al. (HPQCD, MILC	C, UKQCD Collabs.)
AUBIN 0)4A	PR D70 114501	C. Aubin et al.	(MILC Collab.)
AOKI 0)3	PR D67 034503	S. Aoki <i>et al.</i>	(CP-PACS Collab.)
AOKI 0)3B	PR D68 054502	S. Aoki <i>et al.</i>	(CP-PACS Collab.)
BECIREVIC 0)3	PL B558 69	D. Becirevic, V. Lubicz, C. Tarantino	
CHIU 0)3	NP B673 217	TW. Chiu, TH. Hsieh	
GAMIZ 0)3	JHEP 0301 060	E. Gamiz <i>et al.</i>	
NELSON 0)3	PRL 90 021601	D. Nelson, G.T. Fleming, G.W. Kilcup	
ALIKHAN 0)2	PR D65 054505	A. Ali Khan <i>et al.</i>	(CP-PACS Collab.)
Also 0)3	PR D67 059901 (erratum	n)A. Ali Khan <i>et al.</i>	(CP-PACS Collab.)
CHIU 0)2	PL B538 298	TW. Chiu, TH. Hsieh	
JAMIN 0)2	EPJ C24 237	M. Jamin, J.A. Oller, A. Pich	
)2	PR D65 074013	K. Maltman, J. Kambor	
)1B	EPJ C22 31	S. Chen <i>et al.</i>	
)1	EPJ C20 259	J.G. Koerner, F. Krajewski, A.A. Pivov	arov
MALTMAN 0)1	PL B517 332	K. Maltman, J. Kambor	
AOKI 0	00	PRL 84 238	S. Aoki <i>et al.</i>	(CP-PACS Collab.)
	00	PR D62 054504	M. Goeckeler <i>et al.</i>	
AOKI 9	99	PRL 82 4392	S. Aoki <i>et al.</i>	(JLQCD Collab.)
BARATE 9	99R	EPJ C11 599	R. Barate <i>et al.</i>	(ALEPH Collab.)
MALTMAN 9	99	PL B462 195	K. Maltman	
NARISON 9	99	PL B466 345	S. Narison	
	99	JHEP 9910 004	A. Pich, J. Prades	
STEELE 9	99	PL B451 201	T.G. Steele, K. Kostuik, J. Kwan	

⁷³ GAO 97 uses electromagnetic mass splittings of light mesons.

⁷⁴LEUTWYLER 96 uses a combined fit to $\eta \to 3\pi$ and $\psi' \to J/\psi$ (π,η) decay rates, and the electromagnetic mass differences of the π and K.

⁷⁵ DONOGHUE 92 result is from a combined analysis of meson masses, $\eta \to 3\pi$ using second-order chiral perturbation theory including nonanalytic terms, and $(\psi(2S) \to J/\psi(1S)\pi)/(\psi(2S) \to J/\psi(1S)\eta)$.

 $^{^{76}}$ GERARD 90 uses large N and η - η' mixing.

 $^{^{77}}$ LEUTWYLER 90B determines quark mass ratios using second-order chiral perturbation theory for the meson and baryon masses, including nonanalytic corrections. Also uses Weinberg sum rules to determine L_7 .

 $^{^{78}}$ Three flavor dynamical lattice calculation of pseudoscalar meson masses.

 $^{^{79}}$ MARTEMYANOV 05 determine Q from $\eta \to 3\pi$ decay.

⁸⁰ ANISOVICH 96 find Q from $\eta \to \pi^+ \pi^- \pi^0$ decay using dispersion relations and chiral perturbation theory.

BECIREVIC	98	PL B444 401	D. Becirevic et al.
CHETYRKIN	98	NP B533 473	K.G. Chetyrkin, J.H. Kuehn, A.A. Pivovarov
CUCCHIERI	98	PL B422 212	A. Chucchieri et al.
DOMINGUEZ	98	PL B425 193	C.A. Dominguez, L. Pirovano, K. Schilcher
DOSCH	98	PL B417 173	H.G. Dosch, S. Narison
PRADES	98	NPBPS 64 253	J. Prades
CHETYRKIN	97	PL B404 337	K.G. Chetyrkin, D. Pirjol, K. Schilcher
COLANGELO	97	PL B408 340	P. Colangelo et al.
EICKER	97	PL B407 290	N. Eicker et al. (SESAM Collab.)
GAO	97	PR D56 4115	DN. Gao, B.A. Li, ML. Yan
GOUGH	97	PRL 79 1622	B. Gough et al.
GUPTA	97	PR D55 7203	R. Gupta, T. Bhattacharya
LELLOUCH	97	PL B414 195	L. Lellouch, E. de Rafael, J. Taron
ANISOVICH	96	PL B375 335	A.V. Anisovich, H. Leutwyler
LEUTWYLER	96	PL B378 313	H. Leutwyler
BIJNENS	95	PL B348 226	J. Bijnens, J. Prades, E. de Rafael (NORD, BOHR+)
JAMIN	95	ZPHY C66 633	M. Jamin, M. Munz (HEIDT, MUNT)
NARISON	95C	PL B358 113	S. Narison (MONP)
CHOI	92	PL B292 159	K.W. Choi (UCSD)
DONOGHUE	92	PRL 69 3444	J.F. Donoghue, B.R. Holstein, D. Wyler (MASA+)
DONOGHUE	92B	PR D45 892	J.F. Donoghue, D. Wyler (MASA, ZURI, UCSBT)
GERARD	90	MPL A5 391	J.M. Gerard (MPIM)
LEUTWYLER	90B	NP B337 108	H. Leutwyler (BERN)
MALTMAN	90	PL B234 158	K. Maltman, T. Goldman, Stephenson Jr. (YORKC+)