

# LIGHT QUARKS (*u*, *d*, *s*)

OMITTED FROM SUMMARY TABLE

## *u*-QUARK MASS

The *u*-, *d*-, and *s*-quark masses are estimates of so-called “current-quark masses,” in a mass- independent subtraction scheme such as  $\overline{MS}$ . The ratios  $m_u/m_d$  and  $m_s/m_d$  are extracted from pion and kaon masses using chiral symmetry. The estimates of *d* and *u* masses are not without controversy and remain under active investigation. Within the literature there are even suggestions that the *u* quark could be essentially massless. The *s*-quark mass is estimated from SU(3) splittings in hadron masses.

We have normalized the  $\overline{MS}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35. The values of “Our Evaluation” were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
<b><math>2.49^{+0.81}_{-0.79}</math> (1.7–3.3) OUR EVALUATION</b>	See the ideogram below.		
2.01 ± 0.14	1 DAVIES	10	LATT $\overline{MS}$ scheme
2.9 ± 0.2	2 DOMINGUEZ	09	THEO $\overline{MS}$ scheme
2.9 ± 0.8	3 DEANDREA	08	THEO $\overline{MS}$ scheme
3.02 ± 0.33	4 BLUM	07	LATT $\overline{MS}$ scheme
2.7 ± 0.4	5 JAMIN	06	THEO $\overline{MS}$ scheme
1.9 ± 0.2	6 MASON	06	LATT $\overline{MS}$ scheme
2.8 ± 0.2	7 NARISON	06	THEO $\overline{MS}$ scheme
1.7 ± 0.3	8 AUBIN	04A	LATT $\overline{MS}$ scheme
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
2.9 ± 0.6	9 JAMIN	02	THEO $\overline{MS}$ scheme
2.3 ± 0.4	10 NARISON	99	THEO $\overline{MS}$ scheme
3.9 ± 1.1	11 JAMIN	95	THEO $\overline{MS}$ scheme
3.0 ± 0.7	12 NARISON	95C	THEO $\overline{MS}$ scheme

<sup>1</sup> DAVIES 10 determine  $\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16$  using a lattice computation with dynamical fermions of the pseudoscalar meson masses. Mass  $m_u$  is obtained from this using the value of  $m_c$  from ALLISON 08 and the BAZAVOV 10 values for the light quark mass ratios,  $m_s/\overline{m}$  and  $m_u/m_d$ .

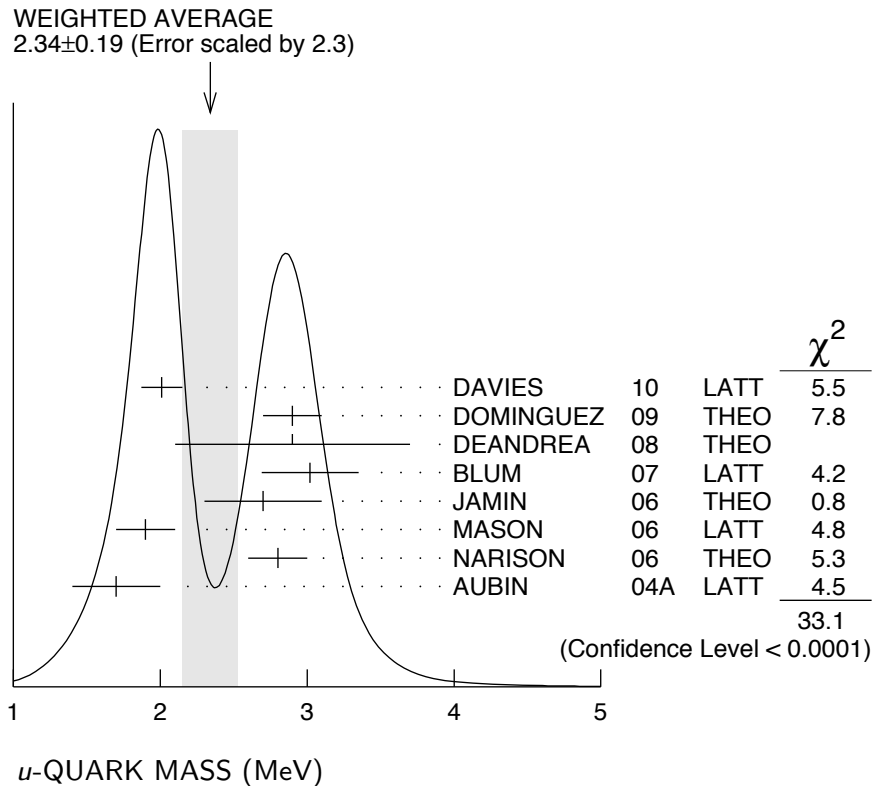
<sup>2</sup> DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order  $\alpha_s^4$ .

<sup>3</sup> DEANDREA 08 determine  $m_u - m_d$  from  $\eta \rightarrow 3\pi^0$ , and combine with the PDG 06 lattice average value of  $m_u + m_d = 7.6 \pm 1.6$  to determine  $m_u$  and  $m_d$ .

<sup>4</sup> BLUM 07 determine quark mass using a QED plus QCD lattice computation with two dynamical flavors of the pseudoscalar meson masses.

<sup>5</sup> JAMIN 06 determine  $m_u(2 \text{ GeV})$  by combining the value of  $m_s$  obtained from the spectral function for the scalar  $K\pi$  form factor with other determinations of the quark mass ratios.

- 6 MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate  $u$  and  $d$  quarks. Perturbative corrections were included at NNLO order. The quark masses  $m_u$  and  $m_d$  were determined from their  $(m_u+m_d)/2$  measurement and AUBIN 04A  $m_u/m_d$  value.
- 7 NARISON 06 uses sum rules for  $e^+e^- \rightarrow$  hadrons to order  $\alpha_s^3$  to determine  $m_s$  combined with other determinations of the quark mass ratios.
- 8 AUBIN 04A employ a partially quenched lattice calculation of the pseudoscalar meson masses.
- 9 JAMIN 02 first calculates the strange quark mass from QCD sum rules using the scalar channel, and then combines with the quark mass ratios obtained from chiral perturbation theory to obtain  $m_u$ .
- 10 NARISON 99 uses sum rules to order  $\alpha_s^3$  for  $\phi$  meson decays to get  $m_s$ , and finds  $m_u$  by combining with sum rule estimates of  $m_u+m_d$  and Dashen's formula.
- 11 JAMIN 95 uses QCD sum rules at next-to-leading order. We have rescaled  $m_u(1\text{ GeV}) = 5.3 \pm 1.5$  to  $\mu = 2\text{ GeV}$ .
- 12 For NARISON 95C, we have rescaled  $m_u(1\text{ GeV}) = 4 \pm 1$  to  $\mu = 2\text{ GeV}$ .



### **d-QUARK MASS**

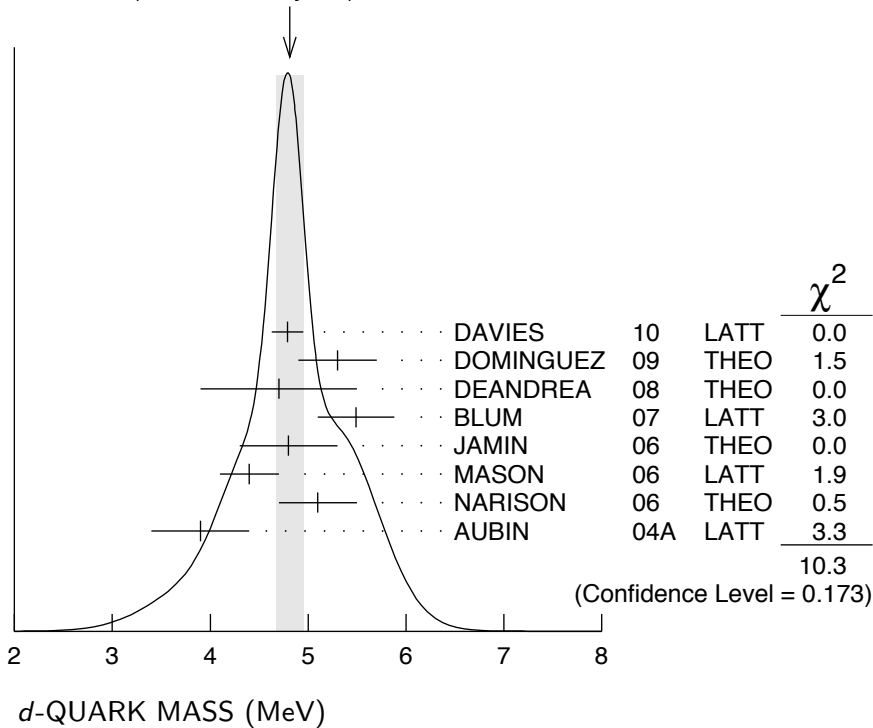
See the comment for the  $u$  quark above.

We have normalized the  $\overline{\text{MS}}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by

dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
<b><math>5.05^{+0.75}_{-0.95}</math></b>	<b>(4.1–5.8) OUR EVALUATION</b> See the ideogram below.		
4.79 ± 0.16	13 DAVIES	10	LATT $\overline{MS}$ scheme
5.3 ± 0.4	14 DOMINGUEZ	09	THEO $\overline{MS}$ scheme
4.7 ± 0.8	15 DEANDREA	08	THEO $\overline{MS}$ scheme
5.49 ± 0.39	16 BLUM	07	LATT $\overline{MS}$ scheme
4.8 ± 0.5	17 JAMIN	06	THEO $\overline{MS}$ scheme
4.4 ± 0.3	18 MASON	06	LATT $\overline{MS}$ scheme
5.1 ± 0.4	19 NARISON	06	THEO $\overline{MS}$ scheme
3.9 ± 0.5	20 AUBIN	04A	LATT $\overline{MS}$ scheme
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
5.2 ± 0.9	21 JAMIN	02	THEO $\overline{MS}$ scheme
6.4 ± 1.1	22 NARISON	99	THEO $\overline{MS}$ scheme
7.0 ± 1.1	23 JAMIN	95	THEO $\overline{MS}$ scheme
7.4 ± 0.7	24 NARISON	95C	THEO $\overline{MS}$ scheme
<p>13 DAVIES 10 determine <math>\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16</math> using a lattice computation with dynamical fermions of the pseudoscalar meson masses. Mass <math>m_d</math> is obtained from this using the value of <math>m_c</math> from ALLISON 08 and the BAZAVOV 10 values for the light quark mass ratios, <math>m_s/\overline{m}</math> and <math>m_u/m_d</math>.</p> <p>14 DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order <math>\alpha_s^4</math>.</p> <p>15 DEANDREA 08 determine <math>m_u - m_d</math> from <math>\eta \rightarrow 3\pi^0</math>, and combine with the PDG 06 lattice average value of <math>m_u + m_d = 7.6 \pm 1.6</math> to determine <math>m_u</math> and <math>m_d</math>.</p> <p>16 BLUM 07 determine quark mass using a QED plus QCD lattice computation with two dynamical flavors of the pseudoscalar meson masses.</p> <p>17 JAMIN 06 determine <math>m_d(2 \text{ GeV})</math> by combining the value of <math>m_s</math> obtained from the spectral function for the scalar <math>K\pi</math> form factor with other determinations of the quark mass ratios.</p> <p>18 MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate <math>u</math> and <math>d</math> quarks. Perturbative corrections were included at NNLO order. The quark masses <math>m_u</math> and <math>m_d</math> were determined from their <math>(m_u + m_d)/2</math> measurement and AUBIN 04A <math>m_u/m_d</math> value.</p> <p>19 NARISON 06 uses sum rules for <math>e^+e^- \rightarrow \text{hadrons}</math> to order <math>\alpha_s^3</math> to determine <math>m_s</math> combined with other determinations of the quark mass ratios.</p> <p>20 AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses, and one-loop perturbative renormalization constant.</p> <p>21 JAMIN 02 first calculates the strange quark mass from QCD sum rules using the scalar channel, and then combines with the quark mass ratios obtained from chiral perturbation theory to obtain <math>m_d</math>.</p> <p>22 NARISON 99 uses sum rules to order <math>\alpha_s^3</math> for <math>\phi</math> meson decays to get <math>m_s</math>, and finds <math>m_d</math> by combining with sum rule estimates of <math>m_u + m_d</math> and Dashen's formula.</p> <p>23 JAMIN 95 uses QCD sum rules at next-to-leading order. We have rescaled <math>m_d(1 \text{ GeV}) = 9.4 \pm 1.5</math> to <math>\mu = 2 \text{ GeV}</math>.</p> <p>24 For NARISON 95C, we have rescaled <math>m_d(1 \text{ GeV}) = 10 \pm 1</math> to <math>\mu = 2 \text{ GeV}</math>.</p>			

WEIGHTED AVERAGE  
 $4.81 \pm 0.14$  (Error scaled by 1.2)



$$\bar{m} = (m_u + m_d)/2$$

See the comments for the  $u$  quark above.

We have normalized the  $\overline{MS}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
<b><math>3.77^{+1.03}_{-0.77}</math> (3.0-4.8) OUR EVALUATION</b>	See the ideogram below.		
3.40 ± 0.07	25	DAVIES 10	LATT $\overline{MS}$ scheme
4.1 ± 0.2	26	DOMINGUEZ 09	THEO $\overline{MS}$ scheme
3.72 ± 0.41	27	ALLTON 08	LATT $\overline{MS}$ scheme
3.85 ± 0.12 ± 0.4	28	BLOSSIER 08	LATT $\overline{MS}$ scheme
3.55 $^{+0.65}_{-0.28}$	29	ISHIKAWA 08	LATT $\overline{MS}$ scheme
4.026 ± 0.048	30	NAKAMURA 08	LATT $\overline{MS}$ scheme
4.25 ± 0.35	31	BLUM 07	LATT $\overline{MS}$ scheme
4.08 ± 0.25 ± 0.42	32	GOCKELER 06	LATT $\overline{MS}$ scheme
4.7 ± 0.2 ± 0.3	33	GOCKELER 06A	LATT $\overline{MS}$ scheme
3.2 ± 0.3	34	MASON 06	LATT $\overline{MS}$ scheme
3.95 ± 0.3	35	NARISON 06	THEO $\overline{MS}$ scheme
2.8 ± 0.3	36	AUBIN 04	LATT $\overline{MS}$ scheme
4.29 ± 0.14 ± 0.65	37	AOKI 03	LATT $\overline{MS}$ scheme
3.223 ± 0.3	38	AOKI 03B	LATT $\overline{MS}$ scheme
4.4 ± 0.1 ± 0.4	39	BECIREVIC 03	LATT $\overline{MS}$ scheme
4.1 ± 0.3 ± 1.0	40	CHIU 03	LATT $\overline{MS}$ scheme

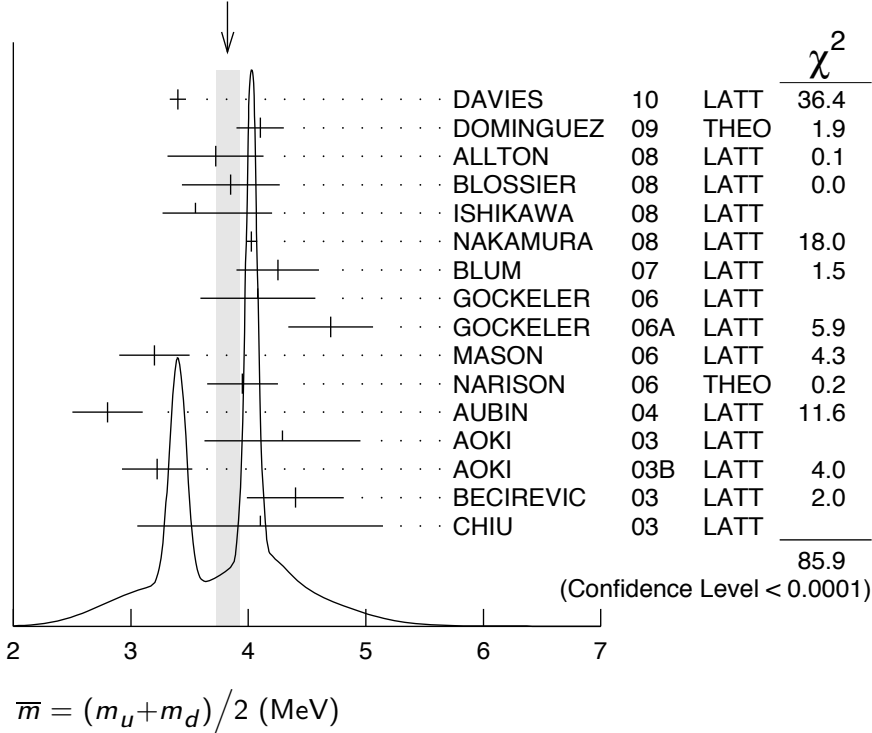
• • • We do not use the following data for averages, fits, limits, etc. • • •

$\geq 4.85 \pm 0.20$	41	DOMINGUEZ...08B	THEO	$\overline{MS}$	scheme
$3.45 \begin{smallmatrix} +0.14 \\ -0.20 \end{smallmatrix}$	42	ALIKHAN	02	LATT	$\overline{MS}$ scheme
$5.3 \pm 0.3$	43	CHIU	02	LATT	$\overline{MS}$ scheme
$3.9 \pm 0.6$	44	MALTMAN	02	THEO	$\overline{MS}$ scheme
$3.9 \pm 0.6$	45	MALTMAN	01	THEO	$\overline{MS}$ scheme
$4.57 \pm 0.18$	46	AOKI	00	LATT	$\overline{MS}$ scheme
$4.4 \pm 2$	47	GOCKELER	00	LATT	$\overline{MS}$ scheme
$4.23 \pm 0.29$	48	AOKI	99	LATT	$\overline{MS}$ scheme
$\geq 2.1$	49	STEELE	99	THEO	$\overline{MS}$ scheme
$4.5 \pm 0.4$	50	BECIREVIC	98	LATT	$\overline{MS}$ scheme
$4.6 \pm 1.2$	51	DOSCH	98	THEO	$\overline{MS}$ scheme
$4.7 \pm 0.9$	52	PRADES	98	THEO	$\overline{MS}$ scheme
$2.7 \pm 0.2$	53	EICKER	97	LATT	$\overline{MS}$ scheme
$3.6 \pm 0.6$	54	GOUGH	97	LATT	$\overline{MS}$ scheme
$3.4 \pm 0.4 \pm 0.3$	55	GUPTA	97	LATT	$\overline{MS}$ scheme
$>3.8$	56	LELLOUCH	97	THEO	$\overline{MS}$ scheme
$4.5 \pm 1.0$	57	BIJNENS	95	THEO	$\overline{MS}$ scheme

- 25 DAVIES 10 determine  $\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16$  using a lattice computation with dynamical fermions of the pseudoscalar meson masses. Mass  $\overline{m}$  is obtained from this using the value of  $m_c$  from ALLISON 08 and the BAZAVOV 10 values for the light quark mass ratio,  $m_s/\overline{m}$ .
- 26 DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order  $\alpha_s^4$ .
- 27 ALLTON 08 use a lattice computation of the  $\pi$ ,  $K$ , and  $\Omega$  masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.
- 28 BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.
- 29 ISHIKAWA 08 use a lattice computation of the light meson spectrum with 2+1 dynamical flavors of  $\mathcal{O}(a)$  improved Wilson quarks, and one-loop perturbative renormalization.
- 30 NAKAMURA 08 do a lattice computation using quenched domain wall fermions and non-perturbative renormalization.
- 31 BLUM 07 determine quark mass using a QED plus QCD lattice computation with two dynamical flavors of the pseudoscalar meson masses.
- 32 GOCKELER 06 use an unquenched lattice computation of the axial Ward Identity with  $N_f = 2$  dynamical light quark flavors, and non-perturbative renormalization, to obtain  $\overline{m}(2 \text{ GeV}) = 4.08 \pm 0.25 \pm 0.19 \pm 0.23 \text{ MeV}$ , where the first error is statistical, the second and third are systematic due to the fit range and force scale uncertainties, respectively. We have combined the systematic errors linearly.
- 33 GOCKELER 06A use an unquenched lattice computation of the pseudoscalar meson masses with  $N_f = 2$  dynamical light quark flavors, and non-perturbative renormalization.
- 34 MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate  $u$  and  $d$  quarks. Perturbative corrections were included at NNLO order.
- 35 NARISON 06 uses sum rules for  $e^+ e^- \rightarrow$  hadrons to order  $\alpha_s^3$  to determine  $m_s$  combined with other determinations of the quark mass ratios.
- 36 AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.
- 37 AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory.

- 38 The errors given in AOKI 03B were  $\begin{matrix} +0.046 \\ -0.069 \end{matrix}$ . We changed them to  $\pm 0.3$  for calculating the overall best values. AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the  $\mathcal{O}(a)$  improved Wilson action.
- 39 BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses  $\mathcal{O}(a)$  improved Wilson action and nonperturbative renormalization.
- 40 CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.
- 41 DOMINGUEZ-CLARIMON 08B obtain an inequality from sum rules for the scalar two-point correlator.
- 42 ALIKHAN 02 uses lattice simulation of the meson and baryon masses with two dynamical flavors and degenerate light quarks.
- 43 CHIU 02 extracts the average light quark mass from quenched lattice simulations using quenched chiral perturbation theory.
- 44 MALTMAN 02 uses finite energy sum rules in the  $ud$  and  $us$  pseudoscalar channels. Other mass values are also obtained by similar methods.
- 45 MALTMAN 01 uses Borel transformed and finite energy sum rules.
- 46 AOKI 00 obtain the light quark masses from a quenched lattice simulation of the meson and baryon spectrum with the Wilson quark action.
- 47 GOCKELER 00 obtained from a quenched lattice computation of the pseudoscalar meson masses using  $\mathcal{O}(a)$  improved Wilson fermions and nonperturbative renormalization.
- 48 AOKI 99 obtain the light quark masses from a quenched lattice simulation of the meson spectrum with the staggered quark action employing the regularization independent scheme.
- 49 STEELE 99 obtain a bound on the light quark masses by applying the Holder inequality to a sum rule. We have converted their bound of  $(m_u+m_d)/2 \geq 3$  MeV at  $\mu=1$  GeV to  $\mu=2$  GeV.
- 50 BECIREVIC 98 compute the quark mass using the Alpha action in the quenched approximation. The conversion from the regularization independent scheme to the  $\overline{\text{MS}}$  scheme is at NNLO.
- 51 DOSCH 98 use sum rule determinations of the quark condensate and chiral perturbation theory to obtain  $9.4 \leq (m_u+m_d)(1 \text{ GeV}) \leq 15.7$  MeV. We have converted to result to  $\mu=2$  GeV.
- 52 PRADES 98 uses finite energy sum rules for the axial current correlator.
- 53 EICKER 97 use lattice gauge computations with two dynamical light flavors.
- 54 GOUGH 97 use lattice gauge computations in the quenched approximation. Correcting for quenching gives  $2.1 < \overline{m} < 3.5$  MeV at  $\mu=2$  GeV.
- 55 GUPTA 97 use Lattice Monte Carlo computations in the quenched approximation. The value for two light dynamic flavors at  $\mu = 2$  GeV is  $2.7 \pm 0.3 \pm 0.3$  MeV.
- 56 LELLOUCH 97 obtain lower bounds on quark masses using hadronic spectral functions.
- 57 BIJNENS 95 determines  $m_u+m_d(1 \text{ GeV}) = 12 \pm 2.5$  MeV using finite energy sum rules. We have rescaled this to 2 GeV.

WEIGHTED AVERAGE  
 $3.82 \pm 0.10$  (Error scaled by 2.8)



### $m_u/m_d$ MASS RATIO

VALUE	DOCUMENT ID	TECN	COMMENT
<b><math>0.494^{+0.106}_{-0.144}</math> (0.35–0.60) OUR EVALUATION</b>			See the ideogram below.
$0.550 \pm 0.031$	58 BLUM	07 LATT	$\overline{MS}$ scheme
$0.43 \pm 0.08$	59 AUBIN	04A LATT	$\overline{MS}$ scheme
$0.410 \pm 0.036$	60 NELSON	03 LATT	$\overline{MS}$ scheme
$0.553 \pm 0.043$	61 LEUTWYLER	96 THEO	Compilation
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
0.44	62 GAO	97 THEO	$\overline{MS}$ scheme
<0.3	63 CHOI	92 THEO	
0.26	64 DONOGHUE	92 THEO	
$0.30 \pm 0.07$	65 DONOGHUE	92B THEO	
0.66	66 GERARD	90 THEO	
0.4 to 0.65	67 LEUTWYLER	90B THEO	
0.05 to 0.78	68 MALTMAN	90 THEO	

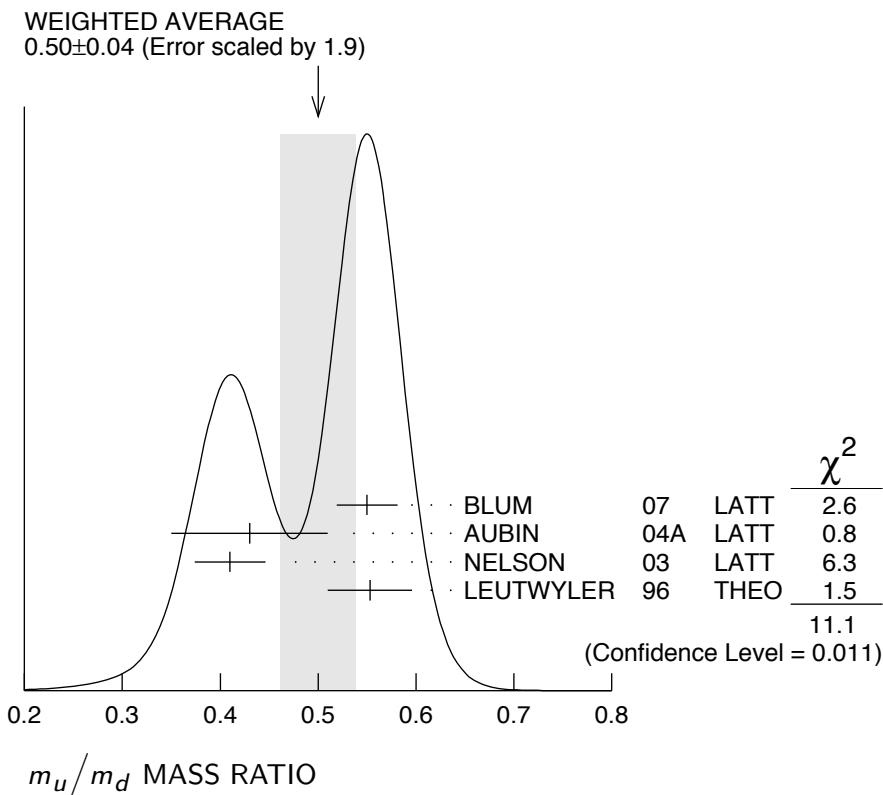
<sup>58</sup> BLUM 07 determine quark mass using a QED plus QCD lattice computation with two dynamical flavors of the pseudoscalar meson masses.

<sup>59</sup> AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses.

<sup>60</sup> NELSON 03 computes coefficients in the order  $p^4$  chiral Lagrangian using a lattice calculation with three dynamical flavors. The ratio  $m_u/m_d$  is obtained by combining this with the chiral perturbation theory computation of the meson masses to order  $p^4$ .

<sup>61</sup> LEUTWYLER 96 uses a combined fit to  $\eta \rightarrow 3\pi$  and  $\psi' \rightarrow J/\psi (\pi, \eta)$  decay rates, and the electromagnetic mass differences of the  $\pi$  and  $K$ .

- 62 GAO 97 uses electromagnetic mass splittings of light mesons.
- 63 CHOI 92 result obtained from the decays  $\psi(2S) \rightarrow J/\psi(1S)\pi$  and  $\psi(2S) \rightarrow J/\psi(1S)\eta$ , and a dilute instanton gas estimate of some unknown matrix elements.
- 64 DONOGHUE 92 result is from a combined analysis of meson masses,  $\eta \rightarrow 3\pi$  using second-order chiral perturbation theory including nonanalytic terms, and  $(\psi(2S) \rightarrow J/\psi(1S)\pi)/(\psi(2S) \rightarrow J/\psi(1S)\eta)$ .
- 65 DONOGHUE 92B computes quark mass ratios using  $(\psi(2S) \rightarrow J/\psi(1S)\pi)/(\psi(2S) \rightarrow J/\psi(1S)\eta)$ , and an estimate of  $L_{14}$  using Weinberg sum rules.
- 66 GERARD 90 uses large  $N$  and  $\eta$ - $\eta'$  mixing.
- 67 LEUTWYLER 90B determines quark mass ratios using second-order chiral perturbation theory for the meson and baryon masses, including nonanalytic corrections. Also uses Weinberg sum rules to determine  $L_7$ .
- 68 MALTMAN 90 uses second-order chiral perturbation theory including nonanalytic terms for the meson masses. Uses a criterion of "maximum reasonableness" that certain coefficients which are expected to be of order one are  $\leq 3$ .



### s-QUARK MASS

See the comment for the  $u$  quark above.

We have normalized the  $\overline{MS}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35.

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
<b><math>101^{+29}_{-21}</math> (80-130) OUR EVALUATION</b>	See the ideogram below.		
$92.4 \pm 1.5$	69 DAVIES	10	LATT $\overline{MS}$ scheme



107.3±11.7	70 ALLTON	08	LATT	$\overline{MS}$	scheme
105 ± 3 ± 9	71 BLOSSIER	08	LATT	$\overline{MS}$	scheme
102 ± 8	72 DOMINGUEZ	08A	THEO	$\overline{MS}$	scheme
90.1 <sup>+17.2</sup> <sub>-6.1</sub>	73 ISHIKAWA	08	LATT	$\overline{MS}$	scheme
105.6± 1.2	74 NAKAMURA	08	LATT	$\overline{MS}$	scheme
119.5± 9.3	75 BLUM	07	LATT	$\overline{MS}$	scheme
105 ± 6 ± 7	76 CHETYRKIN	06	THEO	$\overline{MS}$	scheme
111 ± 6 ±10	77 GOCKELER	06	LATT	$\overline{MS}$	scheme
119 ± 5 ± 8	78 GOCKELER	06A	LATT	$\overline{MS}$	scheme
92 ± 9	79 JAMIN	06	THEO	$\overline{MS}$	scheme
87 ± 6	80 MASON	06	LATT	$\overline{MS}$	scheme
104 ±15	81 NARISON	06	THEO	$\overline{MS}$	scheme
≥ 71 ± 4, ≤ 151 ± 14	82 NARISON	06	THEO	$\overline{MS}$	scheme
96 <sup>+5</sup> <sub>-3</sub> <sup>+16</sup> <sub>-18</sub>	83 BAIKOV	05	THEO	$\overline{MS}$	scheme
81 ±22	84 GAMIZ	05	THEO	$\overline{MS}$	scheme
125 ±28	85 GORBUNOV	05	THEO	$\overline{MS}$	scheme
93 ±32	86 NARISON	05	THEO	$\overline{MS}$	scheme
76 ± 8	87 AUBIN	04	LATT	$\overline{MS}$	scheme
116 ± 6 ± 0.65	88 AOKI	03	LATT	$\overline{MS}$	scheme
84.5 <sup>+12</sup> <sub>-1.7</sub>	89 AOKI	03B	LATT	$\overline{MS}$	scheme
106 ± 2 ± 8	90 BECIREVIC	03	LATT	$\overline{MS}$	scheme
92 ± 9 ±16	91 CHIU	03	LATT	$\overline{MS}$	scheme
117 ±17	92 GAMIZ	03	THEO	$\overline{MS}$	scheme
103 ±17	93 GAMIZ	03	THEO	$\overline{MS}$	scheme

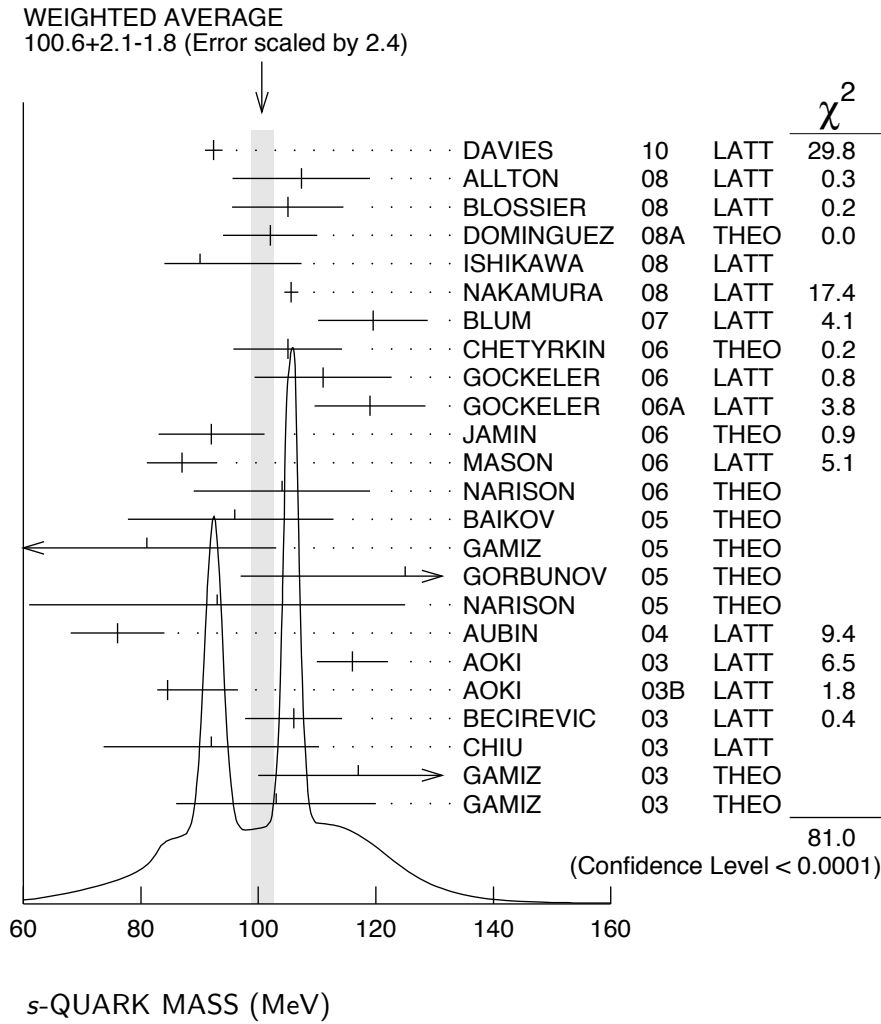
• • • We do not use the following data for averages, fits, limits, etc. • • •

88 <sup>+3</sup> <sub>-6</sub>	94 ALIKHAN	02	LATT	$\overline{MS}$	scheme
115 ± 8	95 CHIU	02	LATT	$\overline{MS}$	scheme
99 ±16	96 JAMIN	02	THEO	$\overline{MS}$	scheme
100 ±12	97 MALTMAN	02	THEO	$\overline{MS}$	scheme
116 <sup>+20</sup> <sub>-25</sub>	98 CHEN	01B	THEO	$\overline{MS}$	scheme
125 ±27	99 KOERNER	01	THEO	$\overline{MS}$	scheme
130 ±15	100 AOKI	00	LATT	$\overline{MS}$	scheme
97 ± 4	101 GARDEN	00	LATT	$\overline{MS}$	scheme
105 ± 4	102 GOCKELER	00	LATT	$\overline{MS}$	scheme
118 ±14	103 AOKI	99	LATT	$\overline{MS}$	scheme
170 <sup>+44</sup> <sub>-55</sub>	104 BARATE	99R	ALEP	$\overline{MS}$	scheme
115 ± 8	105 MALTMAN	99	THEO	$\overline{MS}$	scheme
129 ±24	106 NARISON	99	THEO	$\overline{MS}$	scheme
114 ±23	107 PICH	99	THEO	$\overline{MS}$	scheme
111 ±12	108 BECIREVIC	98	LATT	$\overline{MS}$	scheme
148 ±48	109 CHETYRKIN	98	THEO	$\overline{MS}$	scheme
103 ±10	110 CUCCHIERI	98	LATT	$\overline{MS}$	scheme
115 ±19	111 DOMINGUEZ	98	THEO	$\overline{MS}$	scheme
152.4±14.1	112 CHETYRKIN	97	THEO	$\overline{MS}$	scheme
≥ 89	113 COLANGELO	97	THEO	$\overline{MS}$	scheme

- |                     |              |                                |
|---------------------|--------------|--------------------------------|
| 140 $\pm 20$        | 114 EICKER   | 97 LATT $\overline{MS}$ scheme |
| 95 $\pm 16$         | 115 GOUGH    | 97 LATT $\overline{MS}$ scheme |
| 100 $\pm 21 \pm 10$ | 116 GUPTA    | 97 LATT $\overline{MS}$ scheme |
| >100                | 117 LELLOUCH | 97 THEO $\overline{MS}$ scheme |
| 140 $\pm 24$        | 118 JAMIN    | 95 THEO $\overline{MS}$ scheme |
- 69 DAVIES 10 determine  $\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16$  using a lattice computation with dynamical fermions of the pseudoscalar meson masses. Mass  $m_s$  is obtained from this using the value of  $m_c$  from ALLISON 08.
- 70 ALLTON 08 use a lattice computation of the  $\pi$ ,  $K$ , and  $\Omega$  masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.
- 71 BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.
- 72 DOMINGUEZ 08A make determination from QCD finite energy sum rules for the pseudoscalar two-point function computed to order  $\alpha_s^4$ .
- 73 ISHIKAWA 08 use a lattice computation of the light meson spectrum with 2+1 dynamical flavors of  $\mathcal{O}(a)$  improved Wilson quarks, and one-loop perturbative renormalization.
- 74 NAKAMURA 08 do a lattice computation using quenched domain wall fermions and non-perturbative renormalization.
- 75 BLUM 07 determine quark mass using a QED plus QCD lattice computation with two dynamical flavors of the pseudoscalar meson masses.
- 76 CHETYRKIN 06 use QCD sum rules in the pseudoscalar channel to order  $\alpha_s^4$ .
- 77 GOCKELER 06 use an unquenched lattice computation of the axial Ward Identity with  $N_f = 2$  dynamical light quark flavors, and non-perturbative renormalization, to obtain  $\overline{m}_s(2 \text{ GeV}) = 111 \pm 6 \pm 4 \pm 6 \text{ MeV}$ , where the first error is statistical, the second and third are systematic due to the fit range and force scale uncertainties, respectively. We have combined the systematic errors linearly.
- 78 GOCKELER 06A use an unquenched lattice computation of the pseudoscalar meson masses with  $N_f = 2$  dynamical light quark flavors, and non-perturbative renormalization.
- 79 JAMIN 06 determine  $\overline{m}_s(2 \text{ GeV})$  from the spectral function for the scalar  $K\pi$  form factor.
- 80 MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate  $u$  and  $d$  quarks. Perturbative corrections were included at NNLO order.
- 81 NARISON 06 uses sum rules for  $e^+ e^- \rightarrow \text{hadrons}$  to order  $\alpha_s^3$ .
- 82 NARISON 06 obtains the quoted range from positivity of the spectral functions.
- 83 BAIKOV 05 determines  $\overline{m}_s(M_\tau) = 100^{+5+17}_{-3-19}$  from sum rules using the strange spectral function in  $\tau$  decay. The computations were done to order  $\alpha_s^3$ , with an estimate of the  $\alpha_s^4$  terms. We have converted the result to  $\mu = 2 \text{ GeV}$ .
- 84 GAMIZ 05 determines  $\overline{m}_s(2 \text{ GeV})$  from sum rules using the strange spectral function in  $\tau$  decay. The computations were done to order  $\alpha_s^2$ , with an estimate of the  $\alpha_s^3$  terms.
- 85 GORBUNOV 05 use hadronic tau decays to N<sup>3</sup>LO, including power corrections.
- 86 NARISON 05 determines  $\overline{m}_s(2 \text{ GeV})$  from sum rules using the strange spectral function in  $\tau$  decay. The computations were done to order  $\alpha_s^3$ .
- 87 AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.
- 88 AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory. Determines  $m_s = 113.8 \pm 2.3^{+5.8}_{-2.9}$  using  $K$  mass as input and  $m_s = 142.3 \pm 5.8^{+22}_0$  using  $\phi$  mass as input. We have performed a weighted average of these values.
- 89 AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the  $\mathcal{O}(a)$  improved Wilson action.

- 90 BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses  $\mathcal{O}(a)$  improved Wilson action and nonperturbative renormalization. They also quote  $\bar{m}/m_s=24.3 \pm 0.2 \pm 0.6$ .
- 91 CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.
- 92 GAMIZ 03 determines  $m_s$  from SU(3) breaking in the  $\tau$  hadronic width. The value of  $V_{us}$  is chosen to satisfy CKM unitarity.
- 93 GAMIZ 03 determines  $m_s$  from SU(3) breaking in the  $\tau$  hadronic width. The value of  $V_{us}$  is taken from the PDG.
- 94 ALIKHAN 02 uses lattice simulation of the meson and baryon masses with two dynamical flavors and degenerate light quarks. The above value uses the  $K$ -meson mass to determine  $m_s$ . If the  $\phi$  meson is used, the number changes to  $90^{+5}_{-10}$ .
- 95 CHIU 02 extracts the strange quark mass from quenched lattice simulations using quenched chiral perturbation theory.
- 96 JAMIN 02 calculates the strange quark mass from QCD sum rules using the scalar channel.
- 97 MALTMAN 02 uses finite energy sum rules in the  $ud$  and  $us$  pseudoscalar channels. Other mass values are also obtained by similar methods.
- 98 CHEN 01B uses an analysis of the hadronic spectral function in  $\tau$  decay.
- 99 KOERNER 01 obtain the  $s$  quark mass of  $m_s(m_\tau) = 130 \pm 27(\text{exp}) \pm 9(\text{thy})$  MeV from an analysis of Cabibbo suppressed  $\tau$  decays. We have converted this to  $\mu = 2$  GeV.
- 100 AOKI 00 obtain the light quark masses from a quenched lattice simulation of the meson and baryon spectrum with the Wilson quark action. We have averaged their results of  $m_s = 115.6 \pm 2.3$  and  $m_s = 143.7 \pm 5.8$  obtained using  $m_K$  and  $m_\phi$ , respectively, to normalize the spectrum.
- 101 GARDEN 00 use a quenched lattice computation of the hadron spectrum.
- 102 GOCKELER 00 obtained from a quenched lattice computation of the pseudoscalar meson masses using  $\mathcal{O}(a)$  improved Wilson fermions and nonperturbative renormalization.
- 103 AOKI 99 obtain the light quark masses from a quenched lattice simulation of the meson spectrum with the Staggered quark action employing the regularization independent scheme. We have averaged their results of  $m_s = 106.0 \pm 7.1$  and  $m_s = 129 \pm 12$  obtained using  $m_K$  and  $m_\phi$ , respectively, to normalize the spectrum.
- 104 BARATE 99R obtain the strange quark mass from an analysis of the observed mass spectra in  $\tau$  decay. We have converted their value of  $m_s(m_\tau) = 176^{+46}_{-57}$  MeV to  $\mu = 2$  GeV.
- 105 MALTMAN 99 determines the strange quark mass using finite energy sum rules.
- 106 NARISON 99 uses sum rules to order  $\alpha_s^3$  for  $\phi$  meson decays.
- 107 PICH 99 obtain the  $s$ -quark mass from an analysis of the moments of the invariant mass distribution in  $\tau$  decays.
- 108 BECIREVIC 98 compute the quark mass using the Alpha action in the quenched approximation. The conversion from the regularization independent scheme to the  $\overline{\text{MS}}$  scheme is at NNLO.
- 109 CHETYRKIN 98 uses spectral moments of hadronic  $\tau$  decays to determine  $m_s(1 \text{ GeV}) = 200 \pm 70$  MeV. We have rescaled the result to  $\mu = 2$  GeV.
- 110 CUCCHIERI 98 obtains the quark mass using a quenched lattice computation of the hadronic spectrum.
- 111 DOMINGUEZ 98 uses hadronic spectral function sum rules (to four loops, and including dimension six operators) to determine  $m_s(1 \text{ GeV}) < 155 \pm 25$  MeV. We have rescaled the result to  $\mu = 2$  GeV.
- 112 CHETYRKIN 97 obtains  $205.5 \pm 19.1$  MeV at  $\mu = 1$  GeV from QCD sum rules including fourth-order QCD corrections. We have rescaled the result to 2 GeV.
- 113 COLANGELO 97 is QCD sum rule computation. We have rescaled  $m_s(1 \text{ GeV}) > 120$  to  $\mu = 2$  GeV.
- 114 EICKER 97 use lattice gauge computations with two dynamical light flavors.

- 115 GOUGH 97 use lattice gauge computations in the quenched approximation. Correcting for quenching gives  $54 < m_s < 92$  MeV at  $\mu=2$  GeV.
- 116 GUPTA 97 use Lattice Monte Carlo computations in the quenched approximation. The value for two light dynamical flavors at  $\mu = 2$  GeV is  $68 \pm 12 \pm 7$  MeV.
- 117 LELLOUCH 97 obtain lower bounds on quark masses using hadronic spectral functions.
- 118 JAMIN 95 uses QCD sum rules at next-to-leading order. We have rescaled  $m_s(1 \text{ GeV}) = 189 \pm 32$  to  $\mu = 2$  GeV.



## OTHER LIGHT QUARK MASS RATIOS

### $m_s/m_d$ MASS RATIO

VALUE	DOCUMENT ID	TECN	COMMENT
<b>17 to 22 OUR EVALUATION</b>			
• • • We do not use the following data for averages, fits, limits, etc. • • •			
20.0	119 GAO	97	THEO $\overline{MS}$ scheme
$18.9 \pm 0.8$	120 LEUTWYLER	96	THEO Compilation
21	121 DONOGHUE	92	THEO
18	122 GERARD	90	THEO
18 to 23	123 LEUTWYLER	90B	THEO

- 119 GAO 97 uses electromagnetic mass splittings of light mesons.  
 120 LEUTWYLER 96 uses a combined fit to  $\eta \rightarrow 3\pi$  and  $\psi' \rightarrow J/\psi(\pi, \eta)$  decay rates, and the electromagnetic mass differences of the  $\pi$  and  $K$ .  
 121 DONOGHUE 92 result is from a combined analysis of meson masses,  $\eta \rightarrow 3\pi$  using second-order chiral perturbation theory including nonanalytic terms, and  $(\psi(2S) \rightarrow J/\psi(1S)\pi)/(\psi(2S) \rightarrow J/\psi(1S)\eta)$ .  
 122 GERARD 90 uses large  $N$  and  $\eta$ - $\eta'$  mixing.  
 123 LEUTWYLER 90B determines quark mass ratios using second-order chiral perturbation theory for the meson and baryon masses, including nonanalytic corrections. Also uses Weinberg sum rules to determine  $L_7$ .

### $m_s/\bar{m}$ MASS RATIO

$$\bar{m} \equiv (m_u + m_d)/2$$

VALUE	DOCUMENT ID	TECN	COMMENT
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#### 22 to 30 OUR EVALUATION

• • • We do not use the following data for averages, fits, limits, etc. • • •

28.8±1.65	124 ALLTON	08	LATT $\overline{MS}$ scheme
27.3±0.3 ±1.2	125 BLOSSIER	08	LATT $\overline{MS}$ scheme
23.5±1.5	126 OLLER	07A	THEO
27.4±0.4	127 AUBIN	04	LATT

124 ALLTON 08 use a lattice computation of the  $\pi$ ,  $K$ , and  $\Omega$  masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.

125 BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.

126 OLLER 07A use unitarized chiral perturbation theory to order  $p^4$ .

127 Three flavor dynamical lattice calculation of pseudoscalar meson masses.

### Q MASS RATIO

$$Q \equiv \sqrt{(m_s^2 - \bar{m}^2)/(m_d^2 - m_u^2)}; \quad \bar{m} \equiv (m_u + m_d)/2$$

VALUE	DOCUMENT ID	TECN
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• • • We do not use the following data for averages, fits, limits, etc. • • •

22.8±0.4	128 MARTEMYA...	05	THEO
22.7±0.8	129 ANISOVICH	96	THEO

128 MARTEMYANOV 05 determine  $Q$  from  $\eta \rightarrow 3\pi$  decay.

129 ANISOVICH 96 find  $Q$  from  $\eta \rightarrow \pi^+\pi^-\pi^0$  decay using dispersion relations and chiral perturbation theory.

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MARTEMYA...	05	PR D71 017501	B.V. Martemyanov, V.S. Sopov	
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