

$$\Delta(1905) \ 5/2^+$$

$$I(J^P) = \frac{3}{2}(\frac{5}{2}^+) \text{ Status: } ****$$

Most of the results published before 1975 were last included in our 1982 edition, *Physics Letters* **111B** 1 (1982). Some further obsolete results published before 1984 were last included in our 2006 edition, *Journal of Physics* **G33** 1 (2006).

$\Delta(1905)$ BREIT-WIGNER MASS

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
1855 to 1910 (≈ 1880) OUR ESTIMATE			
1856 ± 6	GUTZ	14	DPWA Multichannel
1861 ± 6	ANISOVICH	12A	DPWA Multichannel
1857.8 ± 1.6	ARNDT	06	DPWA $\pi N \rightarrow \pi N, \eta N$
1910 ± 30	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
1905 ± 20	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
• • • We do not use the following data for averages, fits, limits, etc. • • •			
1818 ± 8	SHRESTHA	12A	DPWA Multichannel
1890 ± 25	¹ ANISOVICH	10	DPWA Multichannel
1855.7 ± 4.2	ARNDT	04	DPWA $\pi N \rightarrow \pi N, \eta N$
1873 ± 77	VRANA	00	DPWA Multichannel
1895 ± 8	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
1850	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
1881 ± 18	MANLEY	92	IPWA $\pi N \rightarrow \pi N \ \& \ N\pi\pi$
1960 ± 40	CANDLIN	84	DPWA $\pi^+ p \rightarrow \Sigma^+ K^+$
1787.0 $^{+6.0}_{-5.7}$	CHEW	80	BPWA $\pi^+ p \rightarrow \pi^+ p$
1830	² LONGACRE	75	IPWA $\pi N \rightarrow N\pi\pi$

$\Delta(1905)$ BREIT-WIGNER WIDTH

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
270 to 400 (≈ 330) OUR ESTIMATE			
325 ± 15	GUTZ	14	DPWA Multichannel
335 ± 18	ANISOVICH	12A	DPWA Multichannel
320.6 ± 8.6	ARNDT	06	DPWA $\pi N \rightarrow \pi N, \eta N$
400 ± 100	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
260 ± 20	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
• • • We do not use the following data for averages, fits, limits, etc. • • •			
278 ± 18	SHRESTHA	12A	DPWA Multichannel
335 ± 30	ANISOVICH	10	DPWA Multichannel
334 ± 22	ARNDT	04	DPWA $\pi N \rightarrow \pi N, \eta N$
461 ± 111	VRANA	00	DPWA Multichannel
354 ± 10	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$

294	ARNDT	95	DPWA	$\pi N \rightarrow N\pi$
327 \pm 51	MANLEY	92	IPWA	$\pi N \rightarrow \pi N$ & $N\pi\pi$
270 \pm 40	CANDLIN	84	DPWA	$\pi^+ p \rightarrow \Sigma^+ K^+$
66.0 ⁺ ₋ 24.0 16.0	CHEW	80	BPWA	$\pi^+ p \rightarrow \pi^+ p$
220	² LONGACRE	75	IPWA	$\pi N \rightarrow N\pi\pi$

$\Delta(1905)$ POLE POSITION

REAL PART

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
1805 to 1835 (\approx 1820) OUR ESTIMATE			
1800 \pm 6	GUTZ	14	DPWA Multichannel
1752 \pm 3 \pm 2	³ SVARC	14	MLS $\pi N \rightarrow \pi N$
1805 \pm 10	ANISOVICH	12A	DPWA Multichannel
1819	ARNDT	06	DPWA $\pi N \rightarrow \pi N, \eta N$
1829	⁴ HOEHLER	93	SPED $\pi N \rightarrow \pi N$
1830 \pm 40	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
1769	SHRESTHA	12A	DPWA Multichannel
1800 \pm 15	ANISOVICH	10	DPWA Multichannel
1825	ARNDT	04	DPWA $\pi N \rightarrow \pi N, \eta N$
1793	VRANA	00	DPWA Multichannel
1832	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
1794	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90
1813 or 1808	⁵ LONGACRE	78	IPWA $\pi N \rightarrow N\pi\pi$

– 2×IMAGINARY PART

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
265 to 300 (\approx 280) OUR ESTIMATE			
290 \pm 15	GUTZ	14	DPWA Multichannel
346 \pm 6 \pm 2	³ SVARC	14	MLS $\pi N \rightarrow \pi N$
300 \pm 15	ANISOVICH	12A	DPWA Multichannel
247	ARNDT	06	DPWA $\pi N \rightarrow \pi N, \eta N$
303	⁴ HOEHLER	93	SPED $\pi N \rightarrow \pi N$
280 \pm 60	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
239	SHRESTHA	12A	DPWA Multichannel
300 \pm 20	ANISOVICH	10	DPWA Multichannel
270	ARNDT	04	DPWA $\pi N \rightarrow \pi N, \eta N$
302	VRANA	00	DPWA Multichannel
254	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
230	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90
193 or 187	⁵ LONGACRE	78	IPWA $\pi N \rightarrow N\pi\pi$

$\Delta(1905)$ ELASTIC POLE RESIDUE**MODULUS $|r|$**

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
19±2	GUTZ	14	DPWA Multichannel
24±1±1	³ SVARC	14	MLS $\pi N \rightarrow \pi N$
20±2	ANISOVICH	12A	DPWA Multichannel
15	ARNDT	06	DPWA $\pi N \rightarrow \pi N, \eta N$
25	HOEHLER	93	SPED $\pi N \rightarrow \pi N$
25±8	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
16	ARNDT	04	DPWA $\pi N \rightarrow \pi N, \eta N$
12	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
14	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90

PHASE θ

<u>VALUE (°)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
− 45± 4	GUTZ	14	DPWA Multichannel
− 114± 1±2	³ SVARC	14	MLS $\pi N \rightarrow \pi N$
− 44± 5	ANISOVICH	12A	DPWA Multichannel
− 30	ARNDT	06	DPWA $\pi N \rightarrow \pi N, \eta N$
− 50±20	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
− 25	ARNDT	04	DPWA $\pi N \rightarrow \pi N, \eta N$
− 4	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
− 40	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90

 $\Delta(1905)$ INELASTIC POLE RESIDUE

The “normalized residue” is the residue divided by $\Gamma_{pole}/2$.

Normalized residue in $N\pi \rightarrow \Delta(1905) \rightarrow \Delta\pi, P$ -wave

<u>MODULUS (%)</u>	<u>PHASE (°)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
25±6	0 ± 15	ANISOVICH	12A	DPWA Multichannel

Normalized residue in $N\pi \rightarrow \Delta(1905) \rightarrow N(1535)\pi$

<u>MODULUS (%)</u>	<u>PHASE (°)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
2.5±1.0	130 ± 35	GUTZ	14	DPWA Multichannel

Normalized residue in $N\pi \rightarrow \Delta(1905) \rightarrow \Delta(1232)\eta$

<u>MODULUS (%)</u>	<u>PHASE (°)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
7±2	40 ± 20	GUTZ	14	DPWA Multichannel

Δ(1905) DECAY MODES

The following branching fractions are our estimates, not fits or averages.

Mode	Fraction (Γ_i/Γ)
Γ_1 $N\pi$	9–15 %
Γ_2 ΣK	
Γ_3 $N\pi\pi$	85–95 %
Γ_4 $\Delta\pi$	<25 %
Γ_5 $\Delta(1232)\pi$, <i>P</i> -wave	
Γ_6 $\Delta(1232)\pi$, <i>F</i> -wave	
Γ_7 $N(1535)\pi$	
Γ_8 $\Delta(1232)\eta$	(4.0±2.0) %
Γ_9 $N\rho$	>60 %
Γ_{10} $N\rho$, <i>S</i> =3/2, <i>P</i> -wave	
Γ_{11} $N\rho$, <i>S</i> =3/2, <i>F</i> -wave	
Γ_{12} $N\rho$, <i>S</i> =1/2, <i>F</i> -wave	
Γ_{13} $N\gamma$	0.012–0.036 %
Γ_{14} $N\gamma$, helicity=1/2	0.002–0.006 %
Γ_{15} $N\gamma$, helicity=3/2	0.01–0.03 %

Δ(1905) BRANCHING RATIOS

$\Gamma(N\pi)/\Gamma_{\text{total}}$	Γ_1/Γ		
VALUE (%)	DOCUMENT ID	TECN	COMMENT
9 to 15 OUR ESTIMATE			
13 ±2	GUTZ	14	DPWA Multichannel
13 ±2	ANISOVICH	12A	DPWA Multichannel
12.2±0.1	ARNDT	06	DPWA $\pi N \rightarrow \pi N, \eta N$
8 ±3	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
15 ±2	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
6 ±1	SHRESTHA	12A	DPWA Multichannel
12 ±3	ANISOVICH	10	DPWA Multichannel
12.0±0.2	ARNDT	04	DPWA $\pi N \rightarrow \pi N, \eta N$
9 ±1	VRANA	00	DPWA Multichannel
12	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
12 ±3	MANLEY	92	IPWA $\pi N \rightarrow \pi N \& N\pi\pi$
11	CHEW	80	BPWA $\pi^+ p \rightarrow \pi^+ p$
$(\Gamma_i\Gamma_f)^{1/2}/\Gamma_{\text{total}}$ in $N\pi \rightarrow \Delta(1905) \rightarrow \Sigma K$		$(\Gamma_1\Gamma_2)^{1/2}/\Gamma$	
VALUE	DOCUMENT ID	TECN	COMMENT
−0.015±0.003	CANDLIN	84	DPWA $\pi^+ p \rightarrow \Sigma^+ K^+$

Note: Signs of couplings from $\pi N \rightarrow N\pi\pi$ analyses were changed in the 1986 edition to agree with the baryon-first convention; the overall phase

ambiguity is resolved by choosing a negative sign for the $\Delta(1620) S_{31}$ coupling to $\Delta(1232)\pi$.

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow \Delta(1905) \rightarrow \Delta(1232)\pi$, *P-wave* $(\Gamma_1 \Gamma_5)^{1/2} / \Gamma$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
• • • We do not use the following data for averages, fits, limits, etc. • • •			
-0.04 ± 0.05	MANLEY	92	IPWA $\pi N \rightarrow \pi N \& N\pi\pi$

$\Gamma(\Delta(1232)\pi, P\text{-wave}) / \Gamma_{\text{total}}$ Γ_5 / Γ

<u>VALUE (%)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
45 ± 14	ANISOVICH	12A	DPWA Multichannel
23 ± 1	VRANA	00	DPWA Multichannel
• • • We do not use the following data for averages, fits, limits, etc. • • •			
28 ± 7	SHRESTHA	12A	DPWA Multichannel

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow \Delta(1905) \rightarrow \Delta(1232)\pi$, *F-wave* $(\Gamma_1 \Gamma_6)^{1/2} / \Gamma$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
$+0.20$	² LONGACRE	75	IPWA $\pi N \rightarrow N\pi\pi$
• • • We do not use the following data for averages, fits, limits, etc. • • •			
$+0.02 \pm 0.03$	MANLEY	92	IPWA $\pi N \rightarrow \pi N \& N\pi\pi$

$\Gamma(\Delta(1232)\pi, F\text{-wave}) / \Gamma_{\text{total}}$ Γ_6 / Γ

<u>VALUE (%)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
44 ± 1	VRANA	00	DPWA Multichannel
• • • We do not use the following data for averages, fits, limits, etc. • • •			
64 ± 8	SHRESTHA	12A	DPWA Multichannel

$\Gamma(N(1535)\pi) / \Gamma_{\text{total}}$ Γ_7 / Γ

<u>VALUE (%)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
< 1	GUTZ	14	DPWA Multichannel

$\Gamma(\Delta(1232)\eta) / \Gamma_{\text{total}}$ Γ_8 / Γ

<u>VALUE (%)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
4 ± 2	GUTZ	14	DPWA Multichannel

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow \Delta(1905) \rightarrow N\rho, S=3/2, P\text{-wave}$ $(\Gamma_1 \Gamma_{10})^{1/2} / \Gamma$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
$+0.30$ to $+0.36$ OUR ESTIMATE			
$+0.33$	² LONGACRE	75	IPWA $\pi N \rightarrow N\pi\pi$
• • • We do not use the following data for averages, fits, limits, etc. • • •			
$+0.33 \pm 0.03$	MANLEY	92	IPWA $\pi N \rightarrow \pi N \& N\pi\pi$

$\Gamma(N\rho, S=3/2, P\text{-wave}) / \Gamma_{\text{total}}$ Γ_{10} / Γ

<u>VALUE (%)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
24 ± 1	VRANA	00	DPWA Multichannel
• • • We do not use the following data for averages, fits, limits, etc. • • •			
< 6	SHRESTHA	12A	DPWA Multichannel

$\Delta(1905)$ PHOTON DECAY AMPLITUDES

Papers on γN amplitudes predating 1981 may be found in our 2006 edition, *Journal of Physics G33* 1 (2006).

$\Delta(1905) \rightarrow N\gamma$, helicity-1/2 amplitude $A_{1/2}$

<u>VALUE (GeV^{-1/2})</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
+0.022±0.005 OUR ESTIMATE			
0.025±0.005	GUTZ	14	DPWA Multichannel
0.020±0.002	DUGGER	13	DPWA $\gamma N \rightarrow \pi N$
0.025±0.004	ANISOVICH	12A	DPWA Multichannel
0.019±0.002	WORKMAN	12A	DPWA $\gamma N \rightarrow \pi N$
0.021±0.004	DUGGER	07	DPWA $\gamma N \rightarrow \pi N$
0.021±0.010	CRAWFORD	83	IPWA $\gamma N \rightarrow \pi N$
0.043±0.020	AWAJI	81	DPWA $\gamma N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
0.066±0.018	SHRESTHA	12A	DPWA Multichannel
0.028±0.012	¹ ANISOVICH	10	DPWA Multichannel
0.018	DRECHSEL	07	DPWA $\gamma N \rightarrow \pi N$
0.022±0.005	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
0.055±0.004	LI	93	IPWA $\gamma N \rightarrow \pi N$

$\Delta(1905) \rightarrow N\gamma$, helicity-3/2 amplitude $A_{3/2}$

<u>VALUE (GeV^{-1/2})</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
-0.045±0.010 OUR ESTIMATE			
-0.050±0.005	GUTZ	14	DPWA Multichannel
-0.049±0.005	DUGGER	13	DPWA $\gamma N \rightarrow \pi N$
-0.049±0.004	ANISOVICH	12A	DPWA Multichannel
-0.038±0.004	WORKMAN	12A	DPWA $\gamma N \rightarrow \pi N$
-0.046±0.005	DUGGER	07	DPWA $\gamma N \rightarrow \pi N$
-0.056±0.028	CRAWFORD	83	IPWA $\gamma N \rightarrow \pi N$
-0.025±0.023	AWAJI	81	DPWA $\gamma N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
-0.223±0.029	SHRESTHA	12A	DPWA Multichannel
-0.042±0.015	¹ ANISOVICH	10	DPWA Multichannel
-0.028	DRECHSEL	07	DPWA $\gamma N \rightarrow \pi N$
-0.045±0.005	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
0.002±0.003	LI	93	IPWA $\gamma N \rightarrow \pi N$

$\Delta(1905)$ FOOTNOTES

¹ ANISOVICH 10 finds an alternate solution for this resonance. The only statistically significant differences are in the Breit-Wigner mass and γp couplings.

² From method II of LONGACRE 75: eyeball fits with Breit-Wigner circles to the T-matrix amplitudes.

³ Fit to the amplitudes of HOEHLER 79.

⁴ See HOEHLER 93 for a detailed discussion of the evidence for and the pole parameters of N and Δ resonances as determined from Argand diagrams of πN elastic partial-wave amplitudes and from plots of the speeds with which the amplitudes traverse the diagrams.

⁵ LONGACRE 78 values are from a search for poles in the unitarized T-matrix. The first (second) value uses, in addition to $\pi N \rightarrow N\pi\pi$ data, elastic amplitudes from a Saclay (CERN) partial-wave analysis.

Δ (1905) REFERENCESFor early references, see *Physics Letters* **111B** 1 (1982).

GUTZ	14	EPJ A50 74	E. Gutz <i>et al.</i>	(CBELSA/TAPS Collab.)
SVARC	14	PR C89 045205	A. Svarc <i>et al.</i>	
DUGGER	13	PR C88 065203	M. Dugger <i>et al.</i>	(CLAS Collab.)
ANISOVICH	12A	EPJ A48 15	A.V. Anisovich <i>et al.</i>	(BONN, PNPI)
SHRESTHA	12A	PR C86 055203	M. Shrestha, D.M. Manley	(KSU)
WORKMAN	12A	PR C86 015202	R. Workman <i>et al.</i>	(GWU)
ANISOVICH	10	EPJ A44 203	A.V. Anisovich <i>et al.</i>	(BONN, PNPI)
DRECHSEL	07	EPJ A34 69	D. Drechsel, S.S. Kamalov, L. Tiator	(MAINZ, JINR)
DUGGER	07	PR C76 025211	M. Dugger <i>et al.</i>	(Jefferson Lab CLAS Collab.)
ARNDT	06	PR C74 045205	R.A. Arndt <i>et al.</i>	(GWU)
PDG	06	JP G33 1	W.-M. Yao <i>et al.</i>	(PDG Collab.)
ARNDT	04	PR C69 035213	R.A. Arndt <i>et al.</i>	(GWU, TRIU)
VRANA	00	PRPL 328 181	T.P. Vrana, S.A. Dytman,, T.-S.H. Lee	(PITT+)
ARNDT	96	PR C53 430	R.A. Arndt, I.I. Strakovsky, R.L. Workman	(VPI)
ARNDT	95	PR C52 2120	R.A. Arndt <i>et al.</i>	(VPI, BRCO)
HOEHLER	93	πN Newsletter 9 1	G. Hohler	(KARL)
LI	93	PR C47 2759	Z.J. Li <i>et al.</i>	(VPI)
MANLEY	92	PR D45 4002	D.M. Manley, E.M. Saleski	(KSA) IJP
Also		PR D30 904	D.M. Manley <i>et al.</i>	(VPI)
ARNDT	91	PR D43 2131	R.A. Arndt <i>et al.</i>	(VPI, TELE) IJP
CANDLIN	84	NP B238 477	D.J. Candlin <i>et al.</i>	(EDIN, RAL, LOWC)
CRAWFORD	83	NP B211 1	R.L. Crawford, W.T. Morton	(GLAS)
PDG	82	PL 111B 1	M. Roos <i>et al.</i>	(HELSE, CIT, CERN)
AWAJI	81	Bonn Conf. 352	N. Awaji, R. Kajikawa	(NAGO)
Also		NP B197 365	K. Fujii <i>et al.</i>	(NAGO)
CHEW	80	Toronto Conf. 123	D.M. Chew	(LBL) IJP
CUTKOSKY	80	Toronto Conf. 19	R.E. Cutkosky <i>et al.</i>	(CMU, LBL) IJP
Also		PR D20 2839	R.E. Cutkosky <i>et al.</i>	(CMU, LBL) IJP
HOEHLER	79	PDAT 12-1	G. Hohler <i>et al.</i>	(KARLT) IJP
Also		Toronto Conf. 3	R. Koch	(KARLT) IJP
LONGACRE	78	PR D17 1795	R.S. Longacre <i>et al.</i>	(LBL, SLAC)
LONGACRE	75	PL 55B 415	R.S. Longacre <i>et al.</i>	(LBL, SLAC) IJP